AD-755 551

OPEN-WIRE TRANSMISSION LINES APPLIED TO THE MEASUREMENT OF THE MACROSCOPIC ELECTRICAL PROPERTIES OF A FOREST REGION

John Taylor, et al

Stanford Research Institute

Prepared for:

Army Electronics Command Advanced Research Projects Agency

October 1971

DISTRIBUTED BY:



National Technical Information Service
U. S. DEPARTMENT OF COMMERCE
5285 Port Royal Road, Springfield Va. 22151



TR ECOM-0220-42 Special Technical Report 42 Reports Control Symbol OSD-1366

OPEN-WIRE TRANSMISSION LINES APPLIED TO THE MEASUREMENT OF THE MACROSCOPIC ELECTRICAL PROPERTIES OF A FOREST REGION

By: JOHN TAYLOR CHING CHUN HAN CHUNG LIEN TIEN GEORGE HAGN

Prepared for:

U.S. ARMY ELECTRONICS COMMAND FORT MONMOUTH, NEW JERSEY 07703

CONTRACT DAAB07-70-C-0220

Approved for public release; distribution unlimited.



Sponsored by:

ADVANCED RESEARCH PROJECTS AGENCY (ARPA Order 371) U.S. ARMY ELECTRONICS COMMAND

STANFORD RESEARCH INSTITUTE Menlo Park, California 94025 · U.S.A.

Reproduced by
NATIONAL TECHNICAL
INFORMATION SERVICE
U.S. Department of Commerce
Springfield VA 22151



70000000 ta	
9115	THE SHIPS F
(:	(1) to (4)
USA 25-77	• •
12716.72 (1947)	
	AVAILAGIR TE EUROPA
A	

NOTICES

Disciplmers

The findings in this report are not to be construed as an official Department of the Army position, unless so designated by other authorized documents.

The citation of trade names and names of manufacturers in this report is not to be construed as official Government indorsement or approval of commercial products or services referenced herein.

Disposition

Destroy this report when it is no longer needed. Do not return it to the originator.

UNCLASSIFIED	•
Security Classification	
DOCUMENT CONT	ROL DATA - R & D
	ennotation must be entered when the overall report is classified)
Stanford Research Institute	AB, REPORT SECURITY CLASSIFICATION
333 Ravenswood Avenue	Unclassified
Menlo Park, California 94025	N/A
3. REPORT TITLE	
OPEN-WIRE TRANSMISSION LINES APPLIED TO T	E MEASUREMENT OF THE MACROSCOPIC
ELECTRICAL PROPERTIES OF A FOREST REGION	
4. DESCRIPTIVE NOTES (Type of report and inclusive dates)	
Special Technical Report 42	
5. AUTHOR(S) (First name, middle initial, last name)	
John Taylor Ching Chun Han Chung Lie	en Tien George Hagn
F. REPORT DATE	78. TOTAL NO. OF PAGES 7b. NO. OF REFS
June 1972	150
SE. CONTRACT OR GRANT NO.	9a. ORIGINATOR'S REPORT NUMBER(S)
DAAB07-70-C-0220	Special Technical Report 42
b. PROJECT NO.	bpecial rechifical keport 42
	SRI Project 8663
c.	9b. OTHER REPORT NO(5) (Any other numbers that may be assigned this report)
d.	
10. DISTRIBUTION STATEMENT	
This document has been approved for public	release and sale. It's distribution is
unlimited.	reaction and bare, it is applicately the
dhlimited.	·
" SUPPLEMENTARY NOTES This work was initiated	12. SPONSORING MILITARY ACTIVITY
under Contract DA36-039 AMC-00040(E) (SRT)	Advanced Research Projects Agency and
Project 4240) and completed under the con-	U.S. Army Electronics Command
tract referenced in line 8a above.	Fort Monmouth, New Jersey 07703

The theoretical capabilities of two-conductor, open-wire transmission lines (OWLs) as probes to measure the macroscopic electrical properties of a forest are examined under the premise that a forest can be represented as a lossy dielectric slab. A laboratory experiment with a line inserted in a relatively homogeneous, isotropic slab of Styrofoam was performed to verify certain approximations in the analysis of such a line when a void (hole) exists in the slab near the line. The effective sensing radius for a 300-ohm line is shown to be about one and one-half line spacings. The limitations of a transmission-line probe for inhomogeneous and anisotropic dielectrics are discussed.

The forest also is considered as a synthetic dielectric composed of lossy scatterers. The equivalent circuit of a short scatterer (length small relative to the RF wavelength) as a load on the transmission line is shown to be a lossy capacitor. The values of capacitance and resistance for isolated trees were measured and observed to depend on (among other things) tree height, diameter, conductivity, and distance from the line. A forest was simulated in the laboratory with wooden bars and also with metal rods positioned at random along a transmission line. The complex dielectric constant of the synthetic forest was deduced from the propagation constant of the line as determined from impedance bridge readings. The results were in reasonable

DD PORM 1473 (PAGE 1)

S/N 0101-807-6801

Ta

Unclassified
Security Classification

13. Abstract (concluded)

agreement with values obtained from a computer program for a transmission line loaded randomly with lossy shunt capacitors of a size and distribution similar to that of the simulated forest. The computer model was used to investigate the effect of the number of scatterers per wavelength along the line, and the electric susceptibility (e - 1) was seen to increase linearly with the number of scatterers per wavelength. A brief investigation of the macroscopic electrical properties of a volume containing living vegetation in South Carolina produced results in general agreement with those already obtained in California, Washington, and Thailand.

It is concluded that a forest can be considered to act as a lossy dielectric slab whose electrical properties can be inferred from measurements with OWL probes--even when significant scatterers (e.g., tree trunks) are present; however, the results of such measurements (and particularly in other cases where anisotropy may be significant) must be interpreted with care. A future experiment is recommended where the measured OWL equivalent circuits of single trees are used--along with forest mensuration data (e.g., tree height, diameter and spacing distributions, etc.)--in the random scatterer computer program to estimate the effective electrical properties of an equivalent forest slab. If the results of these suggested experiments are positive, then a significant step will have been taken toward relating the type of forest descriptions currently being made by environmental scientists to the needs of researchers in the field of radio propagation and communications.

TR ECOM-0220-42 October 1971 Special Technical Report 42 Reports Control Symbol OSD-1366

OPEN-WIRE TRANSMISSION LINES APPLIED TO THE MEASUREMENT OF THE MACROSCOPIC ELECTRICAL PROPERTIES OF A FOREST REGION

By: JOHN TAYLOR CHING CHUN HAN CHUNG LIEN TIEN GEORGE HAGN

Prepared for:

U.S. ARMY ELECTRONICS COMMAND FORT MONMOUTH, NEW JERSEY 07703

CONTRACT DAAB07-70-C-0220

SRI Project 8663

Approved by:

R. F. DALY, Director Telecommunications Department

E. J. MOORE, Executive Director Engineering Systems Division

Approved for public release; distribution unlimited.

Sponsored by:

ADVANCED RESEARCH PROJECTS AGENCY (ARPA Order 371)
U.S. ARMY ELECTRONICS COMMAND

.II.

The theoretical capabilities of two-conductor, open-wire transmission lines (OWLs) as probes to measure the macroscopic electrical properties of a forest are examined under the premise that a forest can be represented as a lossy dielectric slab. A laboratory experiment with a line inserted in a relatively homogeneous, isotropic slab of Styrofoam was performed to verify certain approximations in the analysis of such a line when a void (hole) exists in the slab near the line. The affective sensing radius for a 300-ohm line is shown to be about one and one-half line spacings. The limitations of a transmission-line probe for inhomogeneous and anisotropic dielectrics are discussed.

The forest also is considered as a synthetic dielectric composed of lossy scatterers. The equivalent circuit of a short scatterer (length small relative to the RF wavelength) as a load on the transmission line is shown to be a lossy capacitor. The values of capacitance and resistance for isolated trees were measured and observed to depend on (among other things) tree height, diameter, conductivity, and distance from the line. A forest was simulated in the laboratory with wooden bers and also with metal rods positioned at random along a transmission line. The complex dielectric constant of the synthetic forest was deduced from the propagation constant of the line as determined from impedance bridge readings. The results were in reasonable agreement with values obtained from a computer program for a transmission line loaded randomly with lossy shunt capacitors of a size and distribution similar to that of the simulated forest. The computer model was used to investigate the effect of the number of scatterers per wavelength along the line, and the electric susceptibility ($\epsilon_{_{_{\mathbf{r}}}}$ - 1) was seen to increase linearly with the number of

scatterers per wavelength. A brief investigation of the macroscopic electrical properties of a volume containing living vegetation in South Carolina produced results in general agreement with those already obtained in California, Washington, and Thailand.

It is concluded that a forest can be considered to act as a lossy dielectric slab whose electrical properties can be inferred from measurements with OWL probes—even when significant scatterers (e.g., tree trunks) are present; however, the results of such measurements (and particularly in other cases where anisotropy may be significant) must be interpreted with care. A future experiment is recommended where the measured OWL equivalent circuits of single trees are used—along with forest mensuration data (e.g., tree height, diameter and spacing distributions, etc.)—in the random scatterer computer program to estimate the effective electrical properties of an equivalent forest slab. If the results of the suggested experiments are positive, then a significant step will have been taken toward relating the type of forest descriptions currently being made by environmental scientists to the needs of researchers in the field of radio propagation and communications.

CONTENTS

		•	
ABSTI	rac'i	T	111
List	OF	ILLUSTRATIONS	įx
LIST	OF	TABLES	xait
LIST	O.F	SYMBOLS	,xv
I	IM	PRODUCTION	1
II	TH	EORY OF THE USE OF TRANSMISSION LINES FOR MEASURING R MACROSCOPIC ELECTRICAL PROPERTIES OF HOMOGENROUS,	5
		TROPIC DIELECTRICS	_
	Α.		5
	.B .,	The Short-Circuit TerminationOpen-Circuit Termination Method	. 7
	c.	Variable-LengthFixed-Termination Method of Measuring the Characteristic Impedance and Propagation Constant of a Transmission Line	8
111	IN	HOMOGENEITY LIMITATIONS OF TRANSMISSION-LINE METHODS .	11
	Α.	Relative Power Density around a Two-Wire Transmission Line	11
	B.	Two-Wire Line above a Lessy Half-Space	17
	c.	Effect of Air Space around Line Insorted in Otherwise Homogeneous, Isotropic Dielectric	19
IV	AN	ISOTROPY LIMITATIONS	25
	Α.	Relative Power Dansity for Two Orthogonal Polarizations	25
	В.	Integrated Relative Power Density for Two Orthogonal Polarizations	26
	c.	Conclusion	27
	บ.	Recommendations	29
v	DI	SCRETE SCATTERERS NEAR A TRANSMISSION LINE	31
	A.	Introductory Hemarks	31
	*3	Plan tee acimiring three dominants	39

	C.	Equivalent Admittance of a Single Scatterer near	
		an Open-Wire Transmission Line	. 34
		1. Effect of Longitudinal Position of Scatterer	. 34
		2. Effect of Distance of Scatterer from Line	
		3. Effect of Length of Scatterer	. 35
		4. Effect of Electrical Properties of the	•
		Scatterer	. 41
		5. Equivalent Shunt Admittance of a Single Cut	4.00
		Pine Bough	. 43
		6. Equivalent Shunt Admittance of Living Oak	. 45
		7. Summary of Results on Measurements of	, 40
		Equivalent Shunt Admittance of Single	
		Scatterers	. 45
	_		-
	D.	Mutual Impedance and Coupling Effects	. 49
	E.	Many Scatterers Randomly Distributed about a	
		Transmission Line	. 53
		1. Methods of Approach	. 53
		2. 17-MHz Tosts with Image-Flane Line	-
		•	
		a. Dry Wood Bars	
		b. Wet wood Bars	
		c. Metal Rods	, 60
		3. 17-MHz Tests with 300-Ohm Two-Conductor Line	, 66
		a. Dry Wood Bars	. 66
		b. Wer Wood Bors	
		c. Notal Rods	
		4. Discussion of Results of Laboratory	
		Nultiple-Scatterer Tosts	. 67
		5. Results of heasurements with Tronsmission	
		Lines in Living Vegetation in South Carolina	. 73
VI	CON	CLUSIONS AND RECOMMENDATIONS	. 79
	Α.	Conclusions	. 719
	** '		
	₿.	Recognandations	. 60
DDG	rdix	ADERIVATION OF RELATIVE POWER DESSITY	63
• •			
ppe	nd ix	BRQUIVALENCE OF POWER PLOW IN THE COMPLIES 2 AND.	
		w Planes	. 59
444	. فالعديث	And a second section of the property of the contract of the co	
bbe	ra ix	CDERIVATION OF EQUATION USED FOR COMPUTING PROPAGATION CONSTANT AND PRASE VELOCITY	. 95
		raunumitum bundimis niu rimat valatii , , , , ,	, 90
فززن	nd is	DDERIVATION OF RELATIVE POWER DENSITY IN BOTH	
* * *		x AND y POLARIZATIONS	. 107

Appendix	E	ANAL	ysis	0	F /	AD	DE	D (CAI	PA(IA!			ON A		TI	la:	isi	MISSION			Į					
		LINE	TO	AP	PR	OA	CH	A	G	IVEN :		EFFECTIVE			D	DIELECTRIC												
		CONS	TANI	٠.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	115	
REFERENCE	s.			•	•	•	•	•	•	•	•	•	•	•	•	٠	•	•	•	•	•	•		•		•	123	
distribut	'ION	LIS	r .	•			•	•	•				•	•	•	•		•	•			•	•	ě		•	125	į
DD Form 1	473	}																										

では、1990年には、1990年では、1990年には、1

ILLUSTRATIONS

Pig.	1	Relative Power Density Around an Open-Wire Transmission Line	I.
Fig.	2	Relative Pewer Distribution in the Vicinity of a 300-Ohm Open-Wire Transmission Line	† .
Fig.	3	Relative Power Distribution in the Vicinity of Two-Wire Transmission Lines of Various Characteristic Impedances as a Function of Distance from a Line Nidway Between the Conductors	14
Pig.	4	Relative Power in the Vicinity of the Conductors of a Two-Wire Transmission Line as a Function of Radii about Each Conductor	15
Fig.	5	Propagation Constant versus Height above Wooden Table	2.7
Fig.	6	Propagation Constant versus Height above Aluminum Plate	18
Fig.	7	Characteristic Impedance versus Height above Wooden Table and Aluminum Plate	11
Fig.	Ŗ	Open-Wire Transmission Line in Two-Medium Region .	15
Fig.	9	Fractional Phase Valocity for Different Air Spaces Around on Open-Wire Transmission Line	20
Fig.	10	Schematic Measurement Setup of Image-Plane Line	
Fig.	11	Fractional Phase Velocity as a Function of Power fhrough Air Space Around the Open-Wire Transmission Line.	24
Fig.	12	Relative Power Density in X- and Y-Polarization Around an Open-Wire Transmission Line	.24
yıg.	13	Power in Two Orthogonal Polarizations about a Two-Wire Transmission Line as a Function of	28
# sa	1.2	Characteristic Impedance	3:
Fig.	-	Setup for Image-Plane Line Measurement of Shunt	
4 ## -	10	Admittance of Single Scatterer Perpendicular to Image Plane (and Perpendicular to Line),	31
ŕig.	16	Setup for Image-Flore Line Wedsurement of Shunt Admittance of Single Scatterer Pavallul to Image	•
		Plane (but Perpendicular to Line)	35

Preceding page blank

Fig.	17	Measured Equivalent Shunt Capacitance as a Function of Scatterer Length	41
Fig.	18	Equivalent Shunt Capacitance of Wooden Bars as a Function of Water Content	43
Fig.	19	Test Setup for Measurements on Single Fine Bough	44
Fig.	20	Thotographs of Trees Used for Single-Tree Measurements	46
Fig.	21	Measurement Setup for Isolated-Tree Tests	47
Fig.	22	Random Distributions of Scatterers Used for Measurements	54
Fig.	23	Effective Electrical Constants of Volume Containing Dry Wood BarsCalculated and Measured with 200-Okan Image-Plane Line	57
Fig.	24	Effective Electrical Constants of Volume Containing Dry Wood BarsCalculated and Measured with 135-Ohm Image-Plane Line	59
Fig.	25	Effective Electrical Constants of Volume Containing Wet Wood BarsCalculated and Measured with 150-Ohm Image-Plane Line	61
Fig.	26	Effective Electrical Constants of Volume Containing Metal Rods Perpendicular to Aluminum PlateCalculated and Measured with 150-Ohm Image-Plane Line	63
Fig.		Effective Electrical Constants of Volume Containing Metal Rods Parallel to Aluminum Plate Calculated and Measured with 150-00m MeasurePlane Line.	65
Fig.	28	Effective Electrical Constants of Volume Containing Dry Wood Bars-Calculated and Measured with 300-Ohm Two-Wire Line.	68
<u>.</u> .	29	Effective Electrical Constants of Volume Containing Wet Wood BarsCalculated and Messured with 300-Ohm Two-Wire Line	70
Pic.	30	Effective Electrical Constants of Volume Containing Hetal RodsCalculated and Measured with 300-0hm Two-Wire Line	76
Fij.	31	Six-Ft Pine Trees and Approximate Line Position	74
_		Ten-Pt Pine Trees and Approximate Line Position	75
Pig.		Ten-Ft Comellia Tross and Approximate Line Position	76
	عدد.		ĠĠ

STATE AND STATE SHOW

Fig,	E-1	Equivalent Circuits for Capacitively Loaded	
		Transmission Line	119
Fig.	E-2	Relative Permeability and Permittivity vs. the Number	٠.
		of Capacitors (Scatterers) per Wavelength	120

TABLES

Table I	Power in Circles of Radius, r/b, Centered at Bipolar Centers of Two-Wire Transmission Line	16
Table II	Results of Form Measurements with Image-Plane	01
	Line	23
Table III	Power Distribution Around Two-Wire Transmission Lines for Orthogonal Polarizationsin Parcent	27
Table IV	Spacings and Characteristic Impedance for Two-Wire Line	35
Table V	Equivalent Admittance of Single Wooden Scatterer versus Longitudinal Position on Transmission Line	36
Table VI	Shunt Admittance varsus Distance from Line, Bars Perpendicular to Image Plane	39
Table VII	Shunt Admittance versus Distance from Line, Pars Parallel to Image Plane	38
Table VIII	Equivalent Shrat Admittance of Scatterer near a 300-Ohm Two-Wire Transmission Line versus Longth of Scatterer.	40
Table IX	Equivalent Admittance of Wooden Bars noor o 150-Ohm Image-Plane Transmission Line versus Woisture Content of Bare	42
Table X	Equivalent Shunt Admittonce of Single Pine	4:
Table XI	Equivalent Shunt Adulitance of Isolated Small Ook Trees	48
Table XII	Kutual Coupling Tests with Scatterors in Plane Perpendicular to 150-Uhm Image-Plane Lize	5ú
Table XIII	Mutual Coupling Tests with Scatterers in Plane Parallel to 153-dhm leage-Plane Line	51
Table XIV	Electrical Constants with Dry Wood Sars Massured with 200-Ohm Image-Plane Lies	56
Toble XV	Electrical Constants with Dry Vood Dark Colculated for 200-Ohm Image-Place Lize	Ĵŧ
Table XVI	Electrical Constants with they wood bare Nonsured with 135-Oam Inage-Plane Line	54
	•	

Preceding page blank

Table XVII	Electrical Constants with Dry Wood Bars Calculated for 135-Ohm Image-Plane Line	58
Table XVIII	Electrical Constants with Wet Wood Bars Measured with 150-Ohm Image-Plane Line	; 60
Table XIX	Electrical Constants with Wet Wood Bars Calculated for 150-Ohm Image-Plane Line	61
Table XX	Electrical Constants with Metal Rods Perpendicular to Zero-Potential Plane Measured with 150-Ohm Image-Plane Line	62
Table XXI	Flectrical Constants with Metal Rods Perpendicular to Zero-Potential Plane Calculated for 150-Ohm Image-Plane Line	62
Table XXII	Electrical Constants with Metal Rods Parallel to Image Plane Measured with 150-Ohm Image-Plane Line	64
Table XXIII	Electrical Constants with Netal Rods Parallel to Image Plane Calculated for 150-Ohm Image-Plane Line	64
Tab: XXIV	Electrical Constants with Dry Wood Bers Weasured with 300-Ohm Two-Wire Line	66
Table XXV	Electrical Constants with Dry Wood Bars Calculated for 300-Ohm Two-Wire Line	67
Table XXVI	.lectrical Constants with Wet (15 Percent WC) Wood Bars Measured with 300-Ohm Two-Wire Line,	69
Table XXVII	Electrical Constants with Wet (15 Percent WC) Road Birs Calculated for Sou-Ohm Two-Wire	69
Yable XXVIII	Electrical Canatants with Metal Rods Nemaurad with 300-Ohm Two-Wire Line	71
Table XXIX	Electrics Constants with Metal Rods Calculated for 300-com Two-Wire Lice	71
Table XXX	Field Management of Actual Force: Effective Electrical Froperties with 440-3nm Two-Wiro Line 1944 at 19 Mile in Sean Constitut	59

- @ Dielectric Constant
- 6 Complex Relative Dielectric Constant
- ε' Real Part of ε
- $\epsilon_{r}^{\prime\prime}$ Imaginary Part of ϵ_{r}
- E Relative Dielectric Constant of Air
- μ_ Complex Relative Permeability
- μ Real Part of μ
- $\mu_{\mathbf{r}}^{\prime\prime}$ Imaginary Part of $\mu_{\mathbf{r}}$
- μ Relative Permeability of Air
- 2 Characteristic Impedance of a Transmission Line
- Re Real Part of Z
- X_c Imaginary Part of Z_c
- R Characteristic Impedance of a Transmission Line in Air
- $\mathbf{Z}_{\mathbf{g}_{\mathbf{C}}}$ Input impedance of a Transmission Line Terminated in a Short Circuit
- Z Input Impedance of a Transmission Line Terminated in an Open Circuit
- 2, Intrinsis impedance of Free Space
- y Propa, tion Constant of a Transmission Line
- & Attenuation Constant -- Real Part of y
- 8 Phase Constant-Fing thory Part of y
- o Attenuation Constant Due to Conductor Losses
- 6 Loss Targest
- P Prection of Power Flowing in Vold Region
- k Vareleigth

- [Impedance of the Medium
- [Impedance of Free Space (120 π)
- WC Water Content
- X Electric Susceptibility
- f Wave Frequency
- w Angular (radiam) Wave Frequency
- G Real Part of Equivalent Shunt Admittance
- B Imaginary Part of Equivalent Shunt Admittance
- R Equivalent Shunt Resistance of Scatterer
- C Equivalent Shunt Capacitance of Scatterer
- k Wave Number in Air
- L Center Line of Conductor or Scatterer
- a Radius of Conductors
- b Half the Distance between Conductors
- c Half the Distance between Bipolar Centers of the Conductors
- r Radius of Circle from Center of Bipolar Coominate System (or Center of Cenductor)

I INTRODUCTION

In the study of the propagation of radio waves through a forest, a model has been suggested and demonstrated as feasible in which the forest is represented by one or more layers of dielectric above a flat earth. The purpose of the investigation at the University of South Carolina (the results of which are reported here) was to develop the theory pertaining to the use of open-wire transmission-line (OWL) probes for measuring and calculating the equivalent dielectric constant and loss tangent (or conductivity) of the forest region for use in this propagation model. Preliminary results from this study were reported in Ref. 7.

Many different techniques for the measurement of the dielectric constant and the loss tangent of a continuous medium have been developed. These techniques generally fall into two categories: those which use transmission through a sample and those which use the reflection from the sample. The open-wire transmission-line method discussed in this report belongs to the first category; it has been used to measure the effective wacroscopic electrical properties of forest regions in the United States , , io and in Thailang , 11, 12, 13 However, when the openwire line is used for this purpose, several questions arise which must be answered before the validity of the measuring technique can be established. One such question concerns how well a group of randomly spaced, discrete scatterers can be represented in the model by a single parameter (the complex dielectric constant) and whether or not this parameter has the same significance for plane-wave propagation that it does for a TEM wave--of quasi-TEN wave--on a transmission line. In regard to the measurement of this parameter with a transmission line, several other questions orise. For example, how does the support structure for the line effect the eccuracy of the measurement and what is the relative effect of scatterers at different distances from the line?

References are listed at the end of the report.

One support structure considered for use on this project consisted of a two-wire line covered with a fiberglass cylinder. This type of line could be inserted conveniently into dense vegetation while still maintaining the tolerance on conductor spacing. Unfortunately, since the protective fiberglass cylinder excluded vegetation from the immediate vicinity of the line, the following questions arose: How must the computational formulas be modified to take into account the absence of the forest medium in the immediate vicinity of the line? How is the accuracy of the measurement affected? These questions have been considered and are answered in some detail in this report.

The effect of scatterers near a two-wire transmission line was investigated experimentally in the laboratory and in the field. Dry and wet wooden bars and aluminum reds were used individually and in groups to simulate in the laboratory the effects of tree trunks and/or branches. The measurements on individual scatterers yielded equivalent circuits of the scatterers (as seen by the transmission line) as lumped-constant leads at the location of the scatterer along the line. These equivalent circuits then were used to compute the effects of a random distribution of such scatterers and to infer the effective macroscopic electrical properties of a volume containing these scatterers. Measurements were made on random distributions of these scatterers for comparison with the computed values. Measurements on freshly cut vegetation (tree branches) and living vegetation were made to check the reasonableness of the

This report is organized so that the development of most of the various formulae and equations used are presented in the appendices. Some of these are rather standard and are reproduced for the convenience of the reader. Others were not found in the literature, at least in the form in which they are used here. In Sec. 11 the theory of determining the dielectric constant and loss tangent from transmission-line measurements is reviewed, and the formulae for computation are explained.

Section III is concerned with the power-density distribution in the wave around a two-wire line and the relative effect of inhomogenistics at

different positions as a consequence of the distribution. The effect of the fiberglass support structure is considered in this context. In Sec. IV we consider the power densities in two orthogonal polarizations and the limitations of the measuring line for resolving anisotropic properties of the medium as a result of these distributions. Section V presents measured data which show that individual scatterers of the type we are considering can be represented as lossy capacitors on the transmission line. In Sec. V we also consider the representation of the macroscopic effect of distributions of these scatterers (including small trees) by a single parameter, the complex dielectric constant. Section VI presents the conclusions from this study and the recommendation of an experiment to test the hypothesis: that one can determine the OWL equivalent circuit of a single tree as a function of tree type and geometry (tree diameter, height, branch configuration, distance from line, etc.) by measurement; and, knowing the statistics of a given forest (tree type, height and spacing distributions, etc.), one can compute the effective macroscopic electric constants for that forest considered as a lossy dielectric slab.

II THEORY OF THE USE OF TRANSMISSION LINES FOR MEASURING THE MACROSCOPIC ELECTRICAL PROPERTIES OF HOMOGENEOUS, ISOTROPIC DIELECTRICS

A. General Comments

The macroscopic electrical properties of homogeness, isotropic dielectrics can be adequately described for our purposes by two parameters, the complex relative dielectric constant, $\epsilon_{\rm p}$, and the complex relative permeability, $\mu_{\rm p}$. The two parameters can be computed from the characteristic impedance, $Z_{\rm p}$, and the propagation constant, γ , of a transmission line in which the space between the conductors is filled with the material in question. We will write:

$$c_{\mu} = c_{\mu}' - jc_{\mu}'' = c_{\mu}'(1 - j\delta)$$

$$c_{\mu} = \mu_{\mu}' - j\mu_{\mu}''$$

$$V = 0 + j\beta$$

$$C_{e} = k_{e} + jK_{e}$$

For an opan two-wire line in a dielectric;

$$z_e = \frac{1}{\pi} \sqrt{\frac{E}{\epsilon}} \cosh^{-1}\left(\frac{b}{a}\right)$$

and,

It has not been considered necessary to enperate equations involving complex variables total real and imaginary parts. The facility with which complex numbers and functions can be handled by modern compilers (such as Fortran IV) makes the complex form of the equation more convenient for computational purposes than are the two component equations.

where a is the radius of the conductors and b is half the distance between the conductors. For the same transmission line in air, $\mathbf{Z}_{_{\mathbf{C}}}$ becomes

$$R_{co} = \frac{1}{\pi} - \sqrt{\frac{\mu_o}{\epsilon_o}} \cosh^{-1}\left(\frac{b}{a}\right)$$

and y becomes

Therefore,

$$\frac{z_{c}}{R_{co}} = \sqrt{\frac{r_{r}}{\epsilon_{r}}}$$

and,

$$\frac{\gamma}{k_0} = j / \frac{1}{\mu_r c_r} .$$

Solving these two equations for $\varepsilon_{\mathbf{r}}$ and $\mu_{\mathbf{r}},$ we obtain

$$\epsilon_{r} = -j \frac{\gamma}{k_0} \frac{g_{co}}{z_c}$$

For the special case where

we can find ϵ_{μ} (both ϵ_{μ}' and b) either from

or from

$$\epsilon_{\mathbf{r}} = -\frac{2}{\mathbf{k}^2}$$

From the foregoing we see that the dielectric constant can be easily computed from the measured characteristic impedance and propagation constant of a two-wire line which has been inserted into the material under consideration. There are many methods for determining these parameters, but since impedance bridges are much more convenient to use in the frequency range of interest than are slotted lines, we will restrict our attention to bridge methods. Two commonly used methods are considered in the following section.

B. The Short-Circuit Termination -- Open-Circuit Termination Method

If we denote the input impedance of a section of transmission line terminated in a short circuit by $Z_{\rm sc}$ and that of the same section terminated in an open circuit by $Z_{\rm sc}$ then we can write

apd

where ℓ is the length of the section of line. From these two equations we obtain

Sud

$$v = \frac{1}{2} \tanh^{-1} \left(\frac{2sc}{2ac} \right)^{\frac{1}{2}}$$

Two other forms of the formula for computing y, either of which may be more convenient to use, are:

$$v = \frac{1}{L} \tanh^{-1} \left(\frac{z_{sc}}{z_c} \right)$$

ord

$$y = \frac{1}{2L} \ln \left[\frac{1 + \left(\frac{z_{sc}}{z_{oc}}\right)^{\frac{1}{2}}}{1 - \left(\frac{z_{sc}}{z_{oc}}\right)^{\frac{1}{2}}} \right] .$$

In using this method one usually finds that a line approximately an eighth of a wavelength long yields good results since for this length the magnitude of both the hyperbolic tengent and hyperbolic cotangult are approximately unity and hence the magnitudes of $Z_{\rm oc}$ and $Z_{\rm sc}$ are of the order of $\|Z_{\rm oc}\|_1$ a range in which the accuracy of most bridges is high.

C. Variable-Length--Pixed-Tarmination Method of Measuring the
Characteristic Impedance and Propagation Constant of a
Transmission Line

Another method, based on imposence oridge measurements, of finding the characteristic imposence and propagation constant of a transmission line consists of making two measurements of the imput impedance; for both measurements the line section is terminated in the same imposence, but the length of the section is changed between the measurements. In theory, any termination and any two lengths will suffice, but of course the accuracy will be very dependent on the choice of both length and termination since the thorous lengths and the choice of both length and the input impedance at the bridge terminals. We will illustrate the method with an open-procult termination and two lengths which are in ratio of 1 to 2. This is a convenient combination and the accuracy should be good when the shorter length is about three-sixteenths of a wavelength long. In this case write 2(1) for the input impedance of the chorer section and 2(21) for the input impedance of the longer section.

Then,

 $Z(\ell) = Z_c \text{ ceth } \gamma \ell$

bac

 $Z(2l) = Z_{c} \coth (2\gamma l)$

Jsing the identity

 $\coth 2x = \frac{1}{2} \left(\coth x + \tanh x \right)$

we obtain

$$\frac{Z(2l)}{Z_{c}} = \frac{1}{2} \left[\frac{Z(l)}{Z_{c}} + \frac{Z_{c}}{Z(l)} \right]$$

which leads to

$$z_{e} \cdot \sqrt{z(1)(2z(2L) - z(L))}$$

3,50

$$v = \frac{1}{24} \ln \left\{ \frac{\sqrt{\frac{z(t)}{z(2t)} - z(t)} + 1}{\sqrt{\frac{z(2t)}{z(2t)} - z(t)} - 1} \right\}$$

A. Relative Power Density around a Two-Wire Transmission Line

In the preceding section we assumed that the transmission-line probe would be inserted into a homogeneous, isotropic dielectric. We desire to use this probe, however, to measure the average value of the dielectric constant in an inhomogeneous material. One might ask, then, over how large a volume are we averaging when we make one measurement, or what is the effective volume of the sample measured by the transmission-line probe? To answer these questions we must consider how the power carried in the transmission-line wave is distributed about the line.

A contour plot of the relative power density around the transmission line in a plane normal to the line is shown in Fig. 1 (see Appendices A and B for derivation). The point midway between the conductors was chosen as a reference (0 dB). The coordinates are normalized so that the bipolar centers are at the points $x = \pm 1$, y = 0. With these normalizations the contours are independent of the characteristic impedance of the line. For a line with a particular characteristic impedance we can draw circles with the appropriate centers and radii to show where the conductors would be. These circles will enclose the bipolar centers. All contours or parts of contours which fall within those circles should be disregarded. We see, then, that the effect of increasing the characteristic impedance for a line with fixed spacing is to add high powerdensity contours in the region very near the conductors and thus to incrosse the fraction of the power in this region. The high power-density contours for a line with high characteristic impedance are very meanly circles concentric with the conductor surfaces. For a line of any characteristic impedance the low power-density contours, -15 dB or less, are also almost circular; the latter are concentric about the mid-point between the conductors. This near circularity leads to the concept of "radius of offert" or "sonsing radius" discussed below.

Preceding page blank

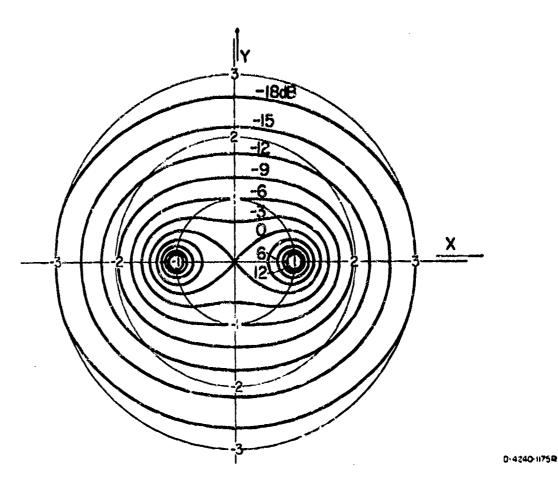
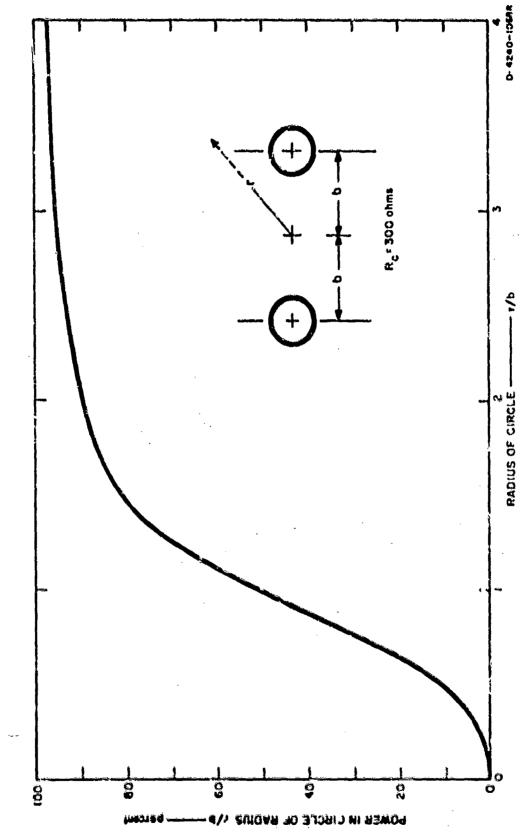


FIG. 1 RELATIVE POWER DENSITY AROUND AN OPEN-WIRE TRANSMISSION LINE

Figure 2 shows the fraction of the pewer flowing through a circle centered midwey between the two conductors of a 300-chm line versus the radius of the circle, r, normalized by half the distance between the conductor centers, b. Figure 3 is a similar plot with the characteristic impedance of the line as a pursmeter, except that the radius is normalized by half the distance between the centers of the bipolar coordinate system. In all cases the circle containing half the power passes through the bimpolar centers of the conductors (in most practical cases the bipolar centers lie slightly inside but near the physical centers of the conductor duetors). For high values of the characteristic impedance this function changes rapidly when the radius is approximately half the conductor spacing. 1842 rapid change with distance is a consequence of the high





Ç

FIG. 2. RELATIVE POWER DISTRIBUTION IN THE VICINITY OF A 300-OHM OPEN-WIRE TRANSMISSION LINE

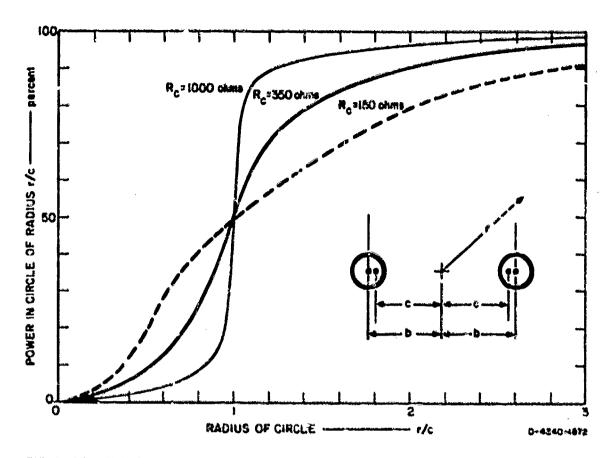


FIG. 3 RELATIVE POWER DISTRIBUTION IN THE VICINITY OF TWO-WIRE TRANSMISSION LINES OF VARIOUS CHARACTERISTIC IMPEDANCES AS A FUNCTION OF DISTANCE FROM A LINE MIDWAY BETWEEN THE CONDUCTORS

power density in the region near the conductors. For a 300-ohm line 95 percent of the power passes through a circle whose radius is 1-1/2 times the conductor spacing. For a 1000-ohm line 95 percent of the power passes through a circle whose radius is five-sixths of the conductor spacing. The power density nutside the 95-percent circle is so low that a scatterer outside this circle would have negligible effect on the measurements. Therefore, one might say that the radius of this circle is the "radius of effect" or "sensing radius" of the transmission-line probe. For a 300-ohm line, since the power-density contours are also nearly circular at the 95-percent circle (passing through x = 3 on Fig. 1), the idea of a radius of effect is measurement. For a 1000-ohm line, however, the radius of the 95-percent circle is not large enough for the power-density contours to approximate circles. The power density varies over a 9 dB range on this circle (passing through x = 1.67 on Fig. 1) on

a 1007-ohm line, and the concept of radius of effect is not particularly meaningful.

Figure 4 shows the fraction of the power flowing through two circles of equal radius centered at the conductor centers versus the radius of the circles. To simplify the computations, circles centered at the bipolar centers were used (see Table I), but for the range of values of characteristic impedance shown, the approximation to circles centered at the conductor centers is excellent. For a characteristic impedance of 300 ohms 50 percent of the power flows through the two circles whose

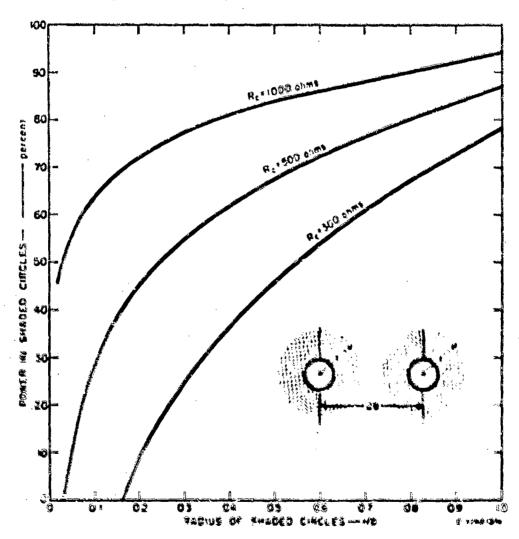


FIG. 4 RELATIVE POWER IN THE VICINITY OF THE CONDUCTORS OF A TWO-WIRE TRANSMISSION LINE AS A PUNCTION OF RADA ABOUT EACH CONDUCTOR

POWER IN CIRCLES OF NADIUL r, CENTERED AT BIPOLAR CENTERS OF TWO-WIRE TRANSMISSION LINE

r/b Rc	250	300	350	400	450	500	750	1000
0,65	0,0000	0.000	0.0000	0.0000	0,0165	0.1149	0,4099	0,5574
0,10	0.0000	00000.0	0.0000	0.1020	0.2017	0.2816	0.5210	0,6408
0.15	0.0000	0.0000	0.1134	0.2242	0.3104	0.3794	0.5862	0.6897
0,20	0.0000	0.0818	0.2130	0.3113	0.3879	0.4491	0,6327	0.7245
0.25	0000,0	0.1724	0.2806	0.3793	0.4483	0.5034	0.6690	0.7517
0.30	0.0963	0.2469	0.3545	0.4352	0.4979	0.5481	0.6988	0.7741
0.35	0.1725	0,3104	0.4090	0.4828	0.5403	0.5863	0.7242	0.7931
0.40	0,2392	0.3660	0.4566	0.5245	0.5773	0.6196	0.7464	0.8098
0.45	0.2987	0.4156	0,4991	0.5617	0.6104	0.6493	0.7662	0.8247
0.50	0.3525	0.4604	0.5375	0.5953	0.6403	0.6763	0.7842	0.8381
0.55	0.4019	0.5016	0.5728	0.6262	0.6677	0.7010	0.8006	0.8505
0.60	0.4477	0.5397	0,6055	0.6548	0.6932	0.7238	0.8159	0.8619
0,65	0.4903	0.5755	0.6361	0.6816	0.7170	0.7453	0.8302	0.8726
0,70	0.5310	0.6091	0,6650	0.7068	0.7394	0.7655	0.8437	0.8827
0,75	0.5694	0.6411	0.6924	0.7308	0.7608	0.7847	0.8565	0.8925
0.80	0.6061	0.6717	0.7166	0.7538	0,7612	0.8030	0.8687	0.9015
0.85	0.6414	0.7012	0.7439	0.7759	8008,0	0.8207	0.8805	0.9104
0.90	0.6757	0.7297	0,7683	0.7973	0.8198	0.8378	0,6919	0,9169
0.55	0.7090	0.7575	0.7921	0.8181	0.6383	0,6545	0,9030	0,9272
69, 1	0.7416	0.7847	0.8154	0.8365	0.6564	0.8706	QE10, 0	0.9354

redius is 0.275 of the line specing and 76 percent of the power flows through the two circles whose redius is one-half of the line specing. For a 1000-ohm line the 50-percent radius is 0.015 of the line specing, and the 64-percent redius is 0.05 of the line specing.

B. Two-Wire Line above a Lossy Half-Space

When we measure the dielectric constant of the forest region there are two obvious inhomogeneities, the effects of which we do not want to include in our average. These are the regions above and below the forest -- the air and the ground. The interface at the forest top would usually be for from the measuring line, but even if it were only a distonce of one line spacing away, one would expect it to have negligible effect since the relative dielectric constant of the forest is pear that of air. The interface at the ground, however, could be expected to have considerable effect since the dielectric constant and loss tangent of the ground are large. For this reason measurements were made in the laboratory to determine how far above a lossy half-space the line must be for the effect of the lossy region to be negligible. First, a 300ohm line (3-3/4-inch spacing) was erected above a wooden table top in a plane parallel to the table, and the open-circuit/short-circuit method was used to determine the propagation constant and the characteristic impedance as a function of height of the line above the table. The tests were then repeated over an aluminum plate 8 ft by 3 ft. The results of these tests are shown in Figs. 5, 6, and 7. Notice that the characteristics of the line are relatively independent of height for heights greater than about one line spacing (i.e., r/b > 2), indicating

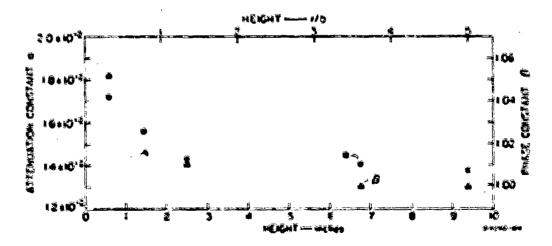
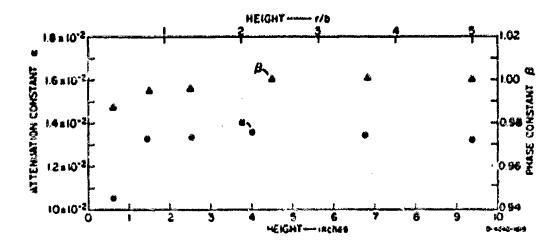


FIG. 5 PROPAGATION CONSTANT WA HEIGHT ABOVE WOODEN TABLE



PIG. 6 PROPAGATION CONSTANT W. HEIGHT ABOVE ALUMINUM PLATE

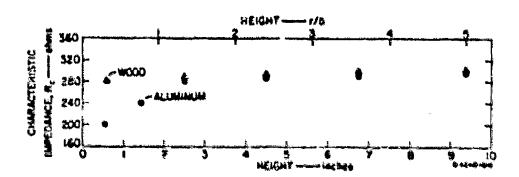


FIG. 7 CHARACTERISTIC IMPEDANCE W. HEIGHT ABOVE WOODEN TABLE AND ALUMINUM PLATE

that forest measurements made with a line placed from ran to one-and-a-half love spacings above the ground would be relatively independent of ground effects. These results are in agreement with the results of field tests with a 300-ohm line over actual ground and also with conclusions about the "radius of effect" of such a line as deduced in the previous section.

[&]quot;W. W. Parker, private communication.

C. Effect of Air Space around Line Inserted in Otherwise Homogeneous, Isotropic Dielectric

Several practicel considerations lead us to consider the effect of excluding the dielectric of interest from the immediate vicinity of the line (i.e., placing the line in proximity to a two-medium region--see Fig. 8). First, it is important to maintain a constant line spacing when inserting the measuring line into vegetation, and, second, we need a line which is convenient to carry and can be easily and quickly set up for measurements. One method suggested for pretecting the line during field use was to encase it in a thin-walled dielectric tube of low permittivity. This technique has the disadvantage of excluding vegetation from the high-field region near the line--particularly the region between the conductors.

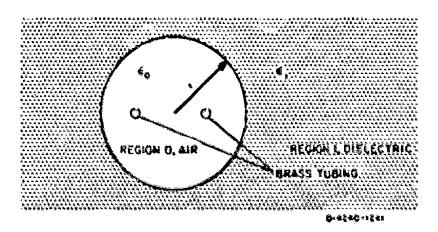
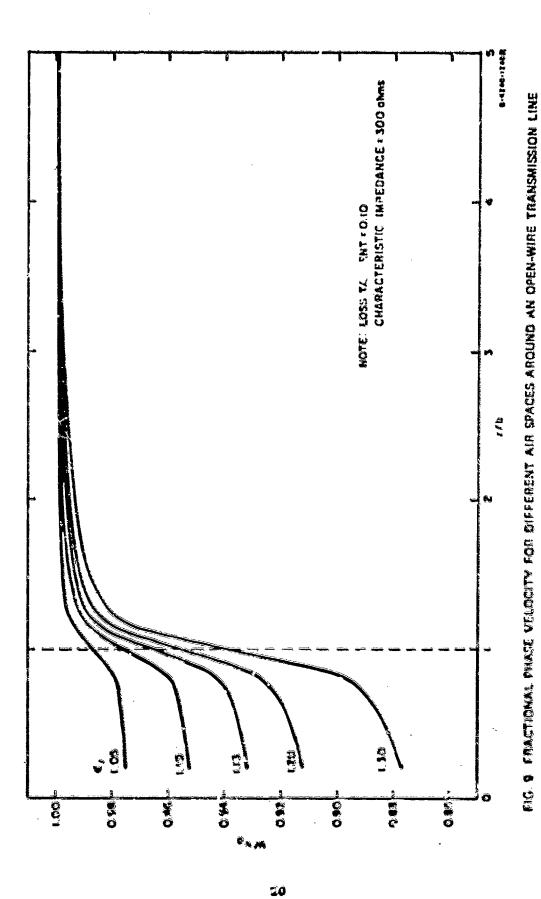


FIG. 8 OPEN-WIRE TRANSMISSION LINE UN TWO-MEDIUM REGION

In order to see the effect of this air space on the propagation constant and phase velocity, these two parameters were computed as functions of the hole diameter using the approximation developed in Appendix 5. The results are shown in Fig. 9, where the phase velocity relative to that of free space is plotted against the hole diameter normalized to the half-spacing of the line. As can be seen from the curves, one could use the measured phase velocity and the known hale Ciameter to compute e... Note, however, that when the hole is large



enough to enclose the conductors (r/b > 1) the curves become quite close together, indicating that a small error in measuring the phase velocity or propagation constant would result in a much larger error in the electric susceptibility $(X_0 = \epsilon_p - 1)$. We therefore recommend that the space between and around the conductors be as uniformly filled with a representative sample of the medium as is practical. But if one must correct for a void region parallel to the axis of the line, the appropriate formula is (see Appendix B):

$$e_y = \frac{-\sqrt{2}(1-p)}{1+\sqrt{2}p}$$

where

F. = the complex relative dielectric constant

y = normalized propagation constant

P = fraction of power flowing in the void region.

As a check on the effect of an air space in the center region of a two-wire line, the phase velocity and propagation constant were determined from measured impedance data on a one-eighth wavelength section of line around which polyurethane form had been poured. A rectangular cavity was cut in the form (see Fig. 10) and was enlarged after each measurement. Instead of a two-wire line, however, a single brase conductor of 5/8-in diameter was used over an aluminum image plane to facilitate the 17-4012 measurements with an unbalanced bridge (General India, GR 1606). An aluminum plate 1-1/2 it by 5 ft was belted to the image plane for use as a short-circuit termination.

The short-circuited and open-circuited impedances of the line were measured in our and found to be

The use of a rectangular hole in the form to theck the theory for the econotry of Fig. 8 in valid (see Appendix C).

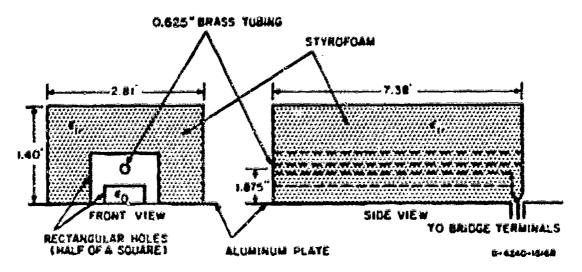


FIG. 10 SCHEMATIC MEASUREMENT SETUP OF MAGE-PLANE LINE

From these measured values, the characteristic impedance in air is cal-

$$Z_c = \left(c_{oc}z_{sc}\right)^{1/2} \approx 154.5$$
 ohms

This result is only slightly higher than the value calculated from theory: 150 ohms (i.e., one-half of the value for a 300-ohm line).

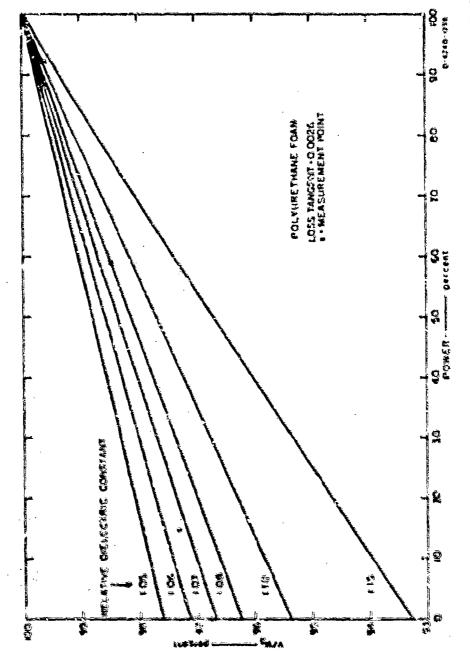
The results of the form measurements are summarised in Table 11, and they are shown—together with the computed curves of phase velocity versus hele size—in Fig. 11. The measured points indicate a dislocitic constant for the form of 1.07. A small sample of the form, when used an the dislocitic of a constant expection, exhibited a dislocitic constant of 1.06.

It has been found experimentally in Thatland by Withen Makerathironia that values of \mathbf{Z}_{q} necessive with this method are elightly higher for short lines than the values computed from theory, but that the difference between theoretically derived and measured values decreases with increasing line longth until the longth is about three wavelengths.

Table II

accepted of foak keanusements with enace-pla line

	-					-		
(1/0) (1/0) (0/0) (0/0)	(0/0)	3# Z .	J [©] Z	Ö	·	ď,	ئى د	ۍ
No tale	Ġ	W. 36 . 1189.4	6°521 - 56'0	£100.0	1.0334 0.9677		1.0678	0.0026
70 **	14.80	20, 700 to 11, 500, 500	0.20 - 1127.53 0.0016 1.0275 0.9732	0.0016	1.0275	0.9732	1.0660	7200,0
1-1/4 * 3-3/4	20,03	. 00 to 1881 . 25. 1 80.	0.05 - 1129.41 0.0020	0,0020	1,0157	0.8846	1.0788	0.0039
2/1-1 × 1/2-2	20. 20	1.34 + 1178,98	0,04 - 1131,76 0,0021		1.0041	0.0959 1.1112 0.0578	6111	0.0578
· · · · · · · · · · · · · · · · · · ·	96.4 8	08.02.18 · 01.0	0.00 - 1132.84	0.0020	1.0014	1.0014 0,9986 1.0708 0.1249	1.0708	0.1249
16 + 20	· 大大、 金田	1.19 . 1176.84	98.55 (1.15 * 1178.84 (0.00 - 1133.50 (0.0622	a .0022	1,0012			



practional phase velocity as a function of power through air space around the open-ware transmission line FIG. 11

IV ANISOTROPY LIMITATIONS

A. Relative Power Density for two Orthogonal Polarizations

In the preceding section we considered a transmission-line probe as a measuring instrument for determining the electrical properties of inhomogeneous but isotropic dielectrics and pointed out some of its limitations. In that discussion we disregarded anisotropic effects. We will now consider a transmission-line probe as an instrument for measuring anisotropic dielectric properties and show that it is not satisfactory for this purpose.

One would expect to be able to resolve anisotropic effects if the field about the probe were predominantly linearly polarized and most of the power was contributed by the component which pointed in a particular direction. The field about a two-wire line is linearly polarized everywhere but varies in direction from point to point. The power densities in two orthogonal polarizations and the fraction of the total power carried in each of them as a function of position around the line is not immediately obvious. It is obvious from the symmetry of the field, however, that if there is a polarization which carries more of the power than any other, then it must be either that in the plane of the conductors or that perpendicular to this plane, since the two orthogonal polarizations at 45° to the plane of the conductors carry equal power. With this fact in mind we computed the power densities and the fraction of the power carried by the two orthogonal polarizations, one in the plane of the conductors and the other perpendicular to it (see Appendix D).

Figure 12 is a plot of contours of constant power density in the xand in the y-polarizations where the conductors are on the x axis. Only
the first quadrant has been plotted. The contours in other quadrants can
be obtained by noting that the curves are symmetric with respect to the
x and y axes. This figure shows that in the region between the two conductors and in the vicinity of the two axes, more of the power is contributed by the x-polarized electric field; and away from those regions
more of the power is contributed by the y-polarized electric field.

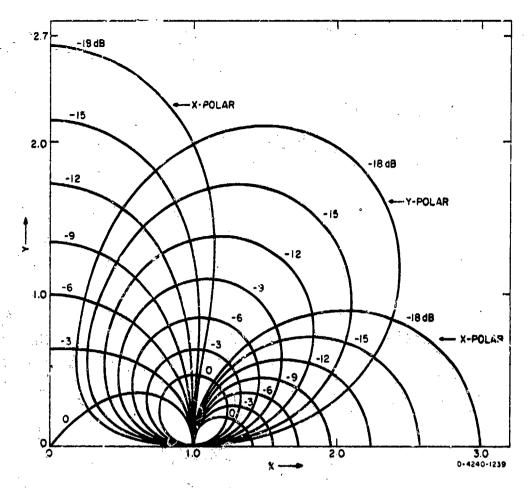


FIG. 12 RELATIVE POWER DENSITY IN X- AND Y-POLARIZATION AROUND AN OPEN-WIRE TRANSMISSION LINE

B. Integrated Relative Power Density for Two Orthogonal Polarizations

The relative power-density expressions for the x (in the plane of the line) and the y (normal to the plane of the line) components, as depicted in Fig. 12, have been integrated to determine the relative power carried in each of these polarizations. In addition, for each polarization the power inside and outside a circle centered midway between the conductors and passing through the centers of the bipolar coordinate system was computed. Table III summarizes the results of the integration for lines of characteristic impedance between 100 and 1000 ohms. It is seen again that half the power is carried within the circle r/c = 1, and that more of the power within that circle is stor—1 in a polarization parallel to the plane containing the centers of the conductors.

Table III

POWER DISTRIBUTION AROUND TWO-WIRE TRANSMISSION LINES
FOR ORTHOGONAL POLARIZATIONS--IN PERCENT

R _C		ide le of = 1	Circ r/c	side le of = 1	Tot	al
(chms)	P X	Py	P _x	Py	Px	Py
100	47.32	2.68	27.01	22.99	74,33	25 ,67
150	44.91	5.09	23.45	26.55	68.36	31.64
200	42.52	7.48	21.94	28.06	64.46	35,54
250	40.39	9.61	21.42	28.58	61.81	38.19
300	38.58	11.42	21.35	28.65	59,93	40.07
500	33.84	16.16	22.13	27.84	56.00	44.00
750	31.00	19.00	23.00	27,00	54.00	46.00
1000	29.5	20,50	23.50	26,50	53,00	47.00

The data of Table III indicate that more of the power about a line is flowing in a polarization parallel to the plane containing the conductors, but that the distribution becomes more even for fixed conductor size as the line spacing is increased (i.e., as the characteristic impedance is increased). Figure 13 shows the ratio of the power in the two orthogonal polarizations to the total power as a function of characteristic impedance.

C. Conclusion

It should be clear from the foregoing discussion that lines of large characteristic impadance cannot be used to resolve the degree of anisotropy of an anisotropic dielectric by simply rotating the configuration 90 degrees. Indeed, it is apparent that a balanced, two-wire transmission line constructed of cylindrical conductors is not a satisfactory instrument for determining the macroscopic anisotropic properties of dielectrics.

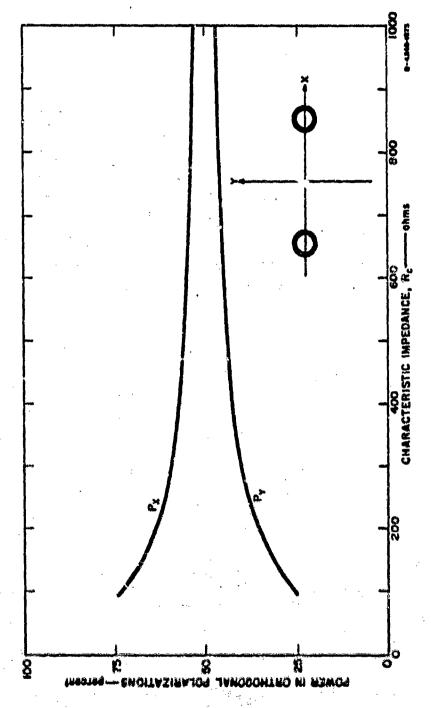


FIG. 13 POWER IN TWO ORTHOGONAL POLARIZATIONS ABOUT A TWO-WIRE TRANSMISSION LINE AS A FUNCTION OF CHARACTERISTIC IMPEDANCE

D. Recommendations

mate of the anisotropy of conductivity can be obtained from measurements of the type described in Ref. 15. Further study is required, however, to develop probes useful for ground-based measurement of the macroscopic, anisotropic properties of the forest. Such probes possibly could be composed of many wires or rods (e.g., multiple-wire transmission lines designed for this purpose). Still another approach is to invert a propagation model and do curve fitting on path-loss data versus separation between transmitter and receiver (at relatively short ranges) and versus antenna heights (at relatively long ranges) and determine what electrical constants for the forest slab are required to give a good fit when horizontal and vertical electric dipoles (or equivalent) are employed.

The propagation model(s) employed would have to allow for anisotropy, and additional model work beyond that given in Refs. 3-5 would be required to generate the appropriate model(s) to be invented. An initial attempt at such model work was made by Dr. John Spence (currently at the University of Rhode Island) while he was with the Jazsky and Dailey Division of Atlantic Research Corp in 1967. This work is summarized in an appendix to "Environmental Effects on Short Range Communication: Report of Technical Study Group," edited by Col. T. W. Doeppner, Joint Advanced Research Projects Agency and Environmental Sciences Service Administration Meeting held in Boulder, Colorado (March 1967).

V DISCRETE SCATTERERS NEAR A TRANSMISSION LINE

A. Introductory Remarks

In this report we have been considering a model for a forest region suitable for explaining and predicting how radio waves propagate through the forest and across the boundaries at the ground and at the tree tops. In our model the forest is considered to be a layer of lossy dielectric -not necessifily homogeneous or isotropic -- which can be characterized by a complex relative dielectric constant, e. . If the medium is not isotropic & will, of course, be a tensor. The present section is concerned with trees as discrete scatterers in an attempt to justify our representation of a large number of discrete scatterers by a continuous medium. In this investigation we have chosen to consider the effect of these scatterers on a wave guided by a two-wire transmission line rather than the effect on a plane wave. We have done this for two reasons: First, because the guided-wave case is a one-dimensional problem which lends itself to analysis by distributed-circuit methods and is also quite easy to study experimentally. Second, because the investigation reported here is concerned with measuring the electrical proporties of the medium, and tho two-wire line shows promise as a measuring instrument for this purpose Since we have considered only the guided wave, the question arises as to whether or not the guided wave is similar enough to the plane wave that the results of our study apply to the plane-wave case; and indeed, whether or not the equivalent dielectric constant measured by transmission-line techniques is the proper value to use for plane-wave propagation. To some extent we will have to leave this question unenswered, but the study does give some insight into the usefulness and validity of our model.

We will consider, then, how the transmission-line wave is affected by scatterers in the vicinity of the line. Since we are interested in the macroscopic properties of the region containing the scatterers, we will assume that the line spacing is wide enough that a ressoluble sample of scatterers is in the region near the line where the field is strong

Preceding page blank

and that there is appreciable probability that a few scatterers (trees) are included in the region between the conductors. The upper frequency limit on the measurement of our macroscopic parameters is then determined by the condition that the line spacing must be very small compared to the wavelength. Under these conditions let us look at the effect of a single one of the scatterers and find its equivalent circuit as a load on the transmission line. Then let us look at pairs of scatterers to see if the equivalent circuit is still valid or if we need to modify it to account for mutual coupling effects. Finally, we will consider random distributions of scatterers loading the line and infer the effective macroscopic electrical properties of the volume containing the scatterers as a function of the average number of scatterers per wavelength along the line.

B. Kessurement Equipment

Ô

0

Two different lines were used for the measurements reported in this section. One was a balanced two-wire line (Fig. 14) with 5/8-in-diameter brass tubing for conductors. The line spacing could be varied in fixed increments to give characteristic impedances with air as a dielectric as

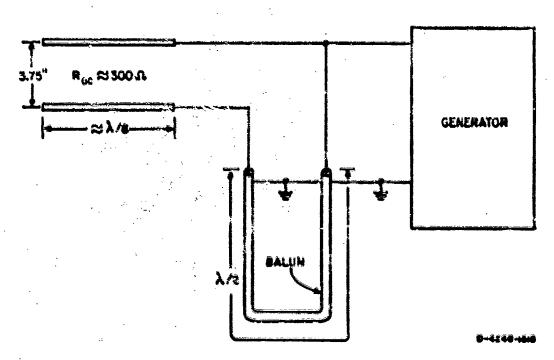


FIG. 14 BALANCED TWO-WIRE LINE

given in Table IV. This line was suspended 15 to 22 inches above a wooden table top, the greatest height for the widest line separation. It was far enough above the table that the table top had negligible effect on the measurements (see Sec. III-B). Since one side of the impedance bridge was at ground potential, it was necessary to use a balanced-to-unbalanced transformer (balun) for measurements with this line. A one-half wavelength section of RG-8/U coaxial transmission line (see Fig. 14) was used for this purpose. The impadance-transformation ratio through this balun transformer was 4 to 1.

Table IV
SPACINGS AND CHARACTERISTIC IMPEDANCE FOR TWO-WIRE LINE

Center-to-Center Spacing (in)	Characteristic Impedance, R _c (ohms)
2.90	270
3,75	300
9,20	400
12.00	440

The other measuring line was the image-plane line corresponding to one-half of the two-wire line (this line was also used for the foam measurements--see Fig. 10). Each of these lines was one-eighth of a wavelength long at the measurement frequency of 17 MHz. The measurements were made with a General Radio 1606 impedance bridge. The signal generator was a Hewlett-Packerd Model 606D and the detector receiver was a Newlett-Packerd Model 417A.

The bridge accuracy was barely sufficient to measure the effect of a single scatterer or a pair of scatterers, and the spread of the data points is primarily due to our imability to make precise measurements. In fact, it was necessary to add a special slow-motion gear mechanism to the diels of the bridge to obtain enough resolution and repeatability for these texts. In spite of this limitation on the accuracy of a single

measurement, enough measurements were made so that the susceptance is sufficiently accurate to show the various effects we are considering. Unfortunately, the scatter in the conductance points is so great that some of the trends are masked.

C. Equivalent Admittance of a Single Scatterer near an Open-Wire Transmission Line

The equivalent shurt admittances of selected scatterers placed in various configurations about a transission line were measured. The acatterers consisted of wet and dry wooden bars, sluminum cylinders, cut vegetation and finally, growing trees. All of the scatterers measured which were not trees or freshly cut parts of trees were cylinders or bars which to some extent could be used to simulate tree trunks or branches.

1. Effect of Longitudinal Position of Scatterer

Cy

0

The shunt admittance should be independent of the longitudinal position of the scatterer on the line except when the scatterer is in the fringing field near the open end of the line. However, the sensitivity, and hence the accuracy, of the measurement is much better when the scatterer is near a high voltage point. For our one-eighth wavelength line the only high voltage region is near the open end. To overcome this dilease, we measured the admittances of several types of scatterers with each of the scatterers at several longitudinal positions pear the open and of the line. From these values of admittance as the scatterer was progressively moved slong the line, it was determined how fer from the open end a scatterer need be so that the admittance would be relatively independent of the longitudinal position. For convenience in weking the measurements and for measurements involving several scattorers, twenty positions with equal specing (e-3/6 in) were worked off slong the line, with position one corresponding to the conding and and position 20 corresponding to the termination end.

Two types of dry whoden here were used for these tests: sir-dried here and oven-dried here. The water (moisture) content of the wat wooden here is expressed in percent (by weight) relative to the oven-dried hers. The water content of the sir-dried here was estimated at about 9 percent relative to the oven-dried here.

wooden bars, and aluminum cylinders are shown in Table V. The 150-ohm image-plane line was used, and the axis of the bar was at right angles to the image plane (Fig. 15). The values of admittances shown are the averages of several measurements with the same configuration. The point at 13-1/8 inches appears to be in error and a little bit high for both the No. 2 set of dry wood bars and the set of metal rods. The difference between Sets 1 and 2 in all cases can be attributed to slight changes in the measurements indicate that consistent results are obtained if the scatterer is at least one line spacing from the open end. For the rest of the measurements involving one or two scatterers, the scatterers were kept at least one line spacing from the end.

2. Effect of Distance of Scatterer from Line

The 150-ohm image-plane line was used for these tests. The 24-1/2-in dry and wet wooden bers (1-1/2 in square) and 1/4-in-diameter eluminum rads were placed 4-3/8 in (position 19-see Fig. 15) from the open end of the line, and the equivalent shunt admittance of the scatterer was measured as the distance from the center line of the scatterer to the center line of the conductor was varied. Two oxientations of scatterer were used: scatterers perpendicular to the image plane (as indicated in Fig. 15) and scatterers parallel to the image plane (see Fig. 16). The results of these measurements are summerized in Tables VI and VII for the two cases where the scatterers were perpendicular to the image plane and parallel to the image plane respectively.

3. Effect of Langth of Scatterer

The tests on the effect of scatterer position around the line (described above in Secs. V-C-1 and V-C-2) were all made with scatterers 24-1/2 in long. It is the purpose of this section to investigate the effect of the length of scatterer for shorter scatterers, and to determine if the equivalent shunt admittance was relatively insensitive to scatterer length for the length used in the previous sections. For these tests, the 300-ohm two-wire line was used, and the scatterers were

Table V

equivalent admittar de of mender monors scapterer vorme honcitedenal fosition of transmission line

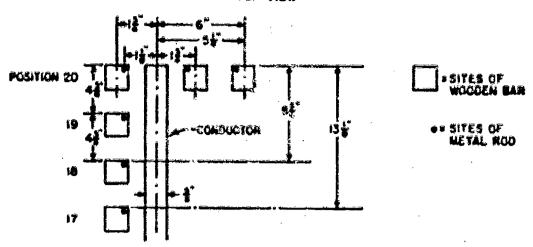
						3441003403	
			Windshipped of		Equivalent	Shume	
			本意名なななない	Montaured	Admittence	Capacitance (C)	
		OURSESSES.	1000	Equipmetont Stuns	of Scatterer on	of Septimen on	
		Section Character	Capacity Co.	Admittance on	300-oth	300-ohe	4
Chatte of	Type of	THE CALLENA	40.4	THE ME OF THE PARTY OF THE PART	No-fire Line	Two-Wire Line	LOSS T. BRODE,
は年の日本の大学の日本の日本	· · · · · · · · · · · · · · · · · · ·	(11)		(nathon)	(pathers)	(p.m.)	O = arc tan (1/4RC)
Contractor	おかり まりからの なのか	0	1/5-1	0.06 . 112,20	0.03 • 16.10	150.0	#70°0
1967	CO present all	年が、	\$ ~ 12 / 4	0,06 * 112.20	0.03 + 16.80	0.057	#00°0
	· · · · · · · · · · · · · · · · · · ·	*/*-	1-304	0,06 + 112,20	0.03 . 14.30	0.037	*00.0
		##-#-##	1-3/4	0.06 + 111.80	0.03 . 15.60	0.054	\$450.0
美国 おおなだ様	(日) 10 10 10 10 10 10 10 10 10 10 10 10 10	0	*/4-1	0,06 * 112,27	0.03 + 36,14	250,0	0.00
	CONTRACTOR SECTION	銀/第二十	1-3/4	0.06 . 113,23	0.03 • 16.42	190.0	0.00¢
	の ままながら 東 コールがある	\$-3.7¢	*****	0,06 + 113.62	0.03 + 16.10	0,063	\$00.0
	* 4 = 4 /WW	13-1/10	1000	D. O.S. 4 M.S. 188	0.03 = 17.59	0.071	900.0
Cacaman	東京 単の名がの あいず	O	\$15-5	0.1 * 12* E	0,43 + 312,49	7.11.0	600.0
1 W. W.	一年 日本	3/X-4	1/2-1	0.1 . 126.1	0.03 - 113,05	- MAT 0	\$0.0
· ·	· 新元日本本 女 · 北京、海上海県	-3.4c	1-204	0,1 . 125,8	*	0.127	*00.0
-	· · · · · · · · · · · · · · · · · · ·	13-1/4	×2-1	0.1 - 127.0	0.05 + \$13.80	0.130	0.004
一番のから数 一世の祖	· · · · · · · · · · · · · · · · · · ·	Э	1-1/4	O.1 * 121,44	LL'air + co.o	001.0	0,004
	· 《 · · · · · · · · · · · · · · · · · ·	2/R-7	7/2-1	0,8 . 139,04	0,05 + 114,52	C. 135	0.003
	「		7/0-1	88.151 + 1.0	0.05 * 315,93	0.149	200.0
	1000年 英	13-1/8	1-3/6-1	0.1 1 132.00	0.05 + 11£.00	0.149	0.003
東京からな 一世の政策	· · · · · · · · · · · · · · · · · · ·	3	2-2/5	CM.TIF . DO.D.	0,00 • 16,40	C10,U	60a'u
-	当//4.17 おりまままままま	# 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	E-1.6素	0.73 + 127, 32	91' 115' * R1'O	0.104	800.6
	· · · · · · · · · · · · · · · · · · ·	サルボー 日	10 mg 3 mg	0,21 - 122,45	0.11 + 111.23	\$01.0	600.0
		# 12m # 1/#	1-1/6	O.T 125.27	C.11 : 112.91	0.120	0.00%
						And the second s	

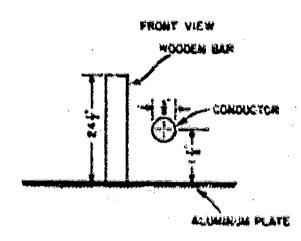
· 第四章 安全的现在分词 医皮肤皮肤 化色色性色谱的 医乳蛋白 人名英格兰斯特特氏 医少别属 医软件 医白红目白眼中的属 经收益条件口程:

West the street continue traight thereto v. 100

Defore soothing, the meeter hare arred for an exem until thate charge to weight with time became negligible.

未未补充的 经设计金属的 医神经性神经 化化二代乙酰胺 化氯化甲丙酯 医生活物 医阿克斯特 医自然抗阻性 医外腺 医自体 医自体 医医神经性神经 计数据记录器 医电子性电影 医电子性神经管 医外外外外 计多数分离 计多数分离 计多数分离 医电子性性神经性神经病





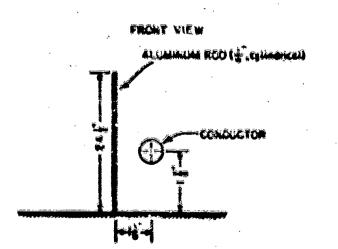
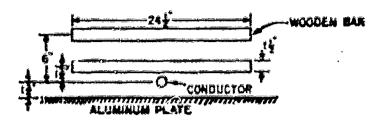
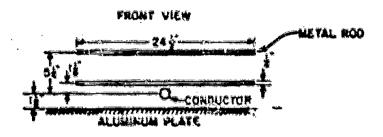
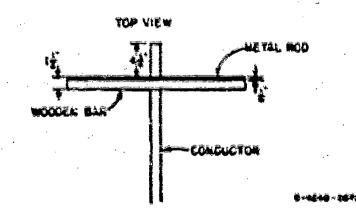


FIG. 16 SETUP FOR WAGE-PLANE LINE MEASUREMENT OF SHURY ADMITTANCE OF SWIGLE SCATTERER PERPENDICULAR TO MAGE PLANE (and perpendicular to make plane)

FRONT VIEW







0

FIG. 16 SETUP FOR IMAGE-PLANE LINE MEASUREMENT OF SHART ADMITTANCE OF SINGLE SCATTERER PARALLEL TO MAGE PLANE THAT PARALLEL

Tables VI

sing of administration which where will likely have verpendicular to exact flake

				thusteness thuse	
				Canar trance (C)	
	Day the section of	日本日本の日本の日本の日本の日本の日本の日本の日本の日本の日本の日本の日本の日本	TO LOLD 1 10 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	of Septions	
	新書をあるのののである。 ののでは、 はいのののできる。 ののでは、 はいののできる。 のので。 の。 の	報子と記事 本色音単される音の音	the meantaining for	STO-1016	
	おおおのであるが、 14 大学 長、	のである。 1900年 190	CHAIR DATA TO SEE OF THE PARTY	Tro-Kire Line	LOSS TRUFBUT
True of Securities	在中的影	Superficients &	CHOCKET	CAC	CANAL CAR (CANAL CAR)
おかか 中をおかめ 東京で	*/**	銀子、子門 * 代子、ひ 2名、宝元 * 公園、〇	第7、参門 * 代学、な	*E0.0	0 105
大学 東京の名をある おのかん	***	10 . O	65.0F * 74.0	500 0	9
(東京日本//各門 歌 自二年//東門 秋 李二年//廣門				1	****
一年日本 子原上本面子 新金子	1//2:-1	10.723 # 14.1	0.00 0.00	0.116	Y 13 15
一 (1) 日本の 日本の 本のの	•	OF 17 . 99 G		ក ក្	1 2 2
在先上的人口一本 电四色八字形 本 如田町八字町					
· · · · · · · · · · · · · · · · · · ·	****	04 . 124 x 125 0	98 CAY # 47 D	201 0	25 C
年// 編月 · 個月 · 新門 · · · · · · · · · · · · · · · · ·	*//#-	新日: 井田 × の事 の	# MY 0 # MY 0	400	, G
ı			MATERIAL PROPERTY OF THE PROPE	The second secon	

Tubbe was

BARTAT ABBITTARES, SPRING DEFRANCE PROF. LIBE, BARTA PARALLER, TO INACE PLANE

A COLOR DE LA COLO					
				Rounds Lene Rhunt	
1.00				CALLES SEARCE ACT	
	おからのはたが 大手	建设的电影的存货的 医线线外形度多种形态	日日 東田本のなる神経の 150mm 日日日本中の中国日本 150mm 150m	CO MONTH CONTROL	
	を の の の の の の の の の の の の の の の の の の の	海流型病果 金沙斯斯名名美国印尼	AL BOATLANET AR	MAN-000	
	新聞記記を必要がきる。 ある み	のでは、またからがきます。 ちゅう 19 19 19 19 19 19 19 19 19 19 19 19 19	MONG - Coffing Trans With the Links of	Two-Cire Line	LORE TREESES
CONTRACTOR OF STREET	C. S. P. D.	€ is writing to \$	Carpeters.)	Cpt)	So at mary then Charles
東京 大田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田田	第 /第四章	£1.45 × 00.00	がない 大学 本 の学・時	7,70° O	71.4 U
(A)	*		20 ET 1 ET C	100	
"我们有一样 关 (1)型//有工作 关 "发门多口的老		N. C. L.			****
ができ 第一位の東京学 第200mm	1 - 27/4	CO CC * 120 *	(C) (M) + (C) + (C)	200	
(A)				£ 2	
34.41/4" + 4.04//4" + 4.44//4"					
金子之間 化水水油 南京北京	₩/3#1	14.200 - 20.00	200	20 0	for Chia
1/18 三八年四十五十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十	\$=1/4	C) . (Sig	14. DE * 156. CO	0.607	8

placed 4-3/8 'n from the open end of the line and 1-3/4 in away from and orthogonal to one conductor of the line. Again 1-1/2-in-square dry and wet wooden bars and aluminum rods were used. Seven different scatterer lengths, from 4-3/8 in to 24-1/2 in, were measured, and the results are summarized in Table VIII. Figure 17 shows the equivalent shunt

Table VIII

EQUIVALENT SHUNT ADMITTANCE OF SCATTERER NEAR A 3GO-OHM TWO-WIRE

TRANSMISSION LINE VERSUS LENGTH OF SCATTERER

		Wassier Law	·	·
	ĺ	Equivalent		
		Shunt	Equivalent Shunt	i
	Length of	Aûmittance on	Capacitance	Loss
Type of	scatterer	Two-Wire Line	of Scatterer	Tangent
Scatterer	(1h)	(µmhos)	(pF)	at 17 MHz
Dry Wooden Bars	4-3/8	0.35 + 14.67	0.043	0.07
with Square	5-1/2	0.36 + j5.14	0,048	0.06
Cross Section	8-7/8	0.75 + j5.15	0,048	0.14
(9 percent WC)	11-1/4	0.75 + 15.60	0.052	0.13
1-1/2" × 1-1/3"	13-1/4	1.28 + 15.82	0.054	0.21
	22-1/2	1.28 + 16.00	0,056	0,21
	24-1/2	1.28 + 16.60	0.060	0,21
Wet Wooden Bars	4-3/8	0.20 + 14.98	0.046	0.04
with Square	5-1/2	0.20 + 15.76	0.053	0.03
Cross Section	8-7/8	0.20 + j6.52	0.031	1.03
(24 percent WC)	11-1/4	0.19 + 18.06	0.075	0.02
1-1/2" × 1-1/2"	13-1/4	0.19 + 110.37	0.097	0,01
1	22-1/2	0.19 + 110.37	0,027	0,01
	24-1/3	0.19 + j10.45	0.097	0,01
Aluminum Rods	4-3/8	0.10 + 54.20	0,039	0.02
1/4" diameter	5-1/2	0.10 + j6.67	0.062	0.01
	8-7/8	0.10 + 18.61	080,0	0,01
	11-1/4	0.10 + 18.64	0.081	0.01
	13-1/4	0.10 + 18.97	0,084	0,01
	22-1/2	0.10 + 110.06	0.094	0.009
	24-1/2	0.10 + 110.06	0.094	0.009

capacitance of the scatterers as a function of scatterer longth. Evidently the length of the scatterers used for the tests of the effect of longitudinal position was adequate.

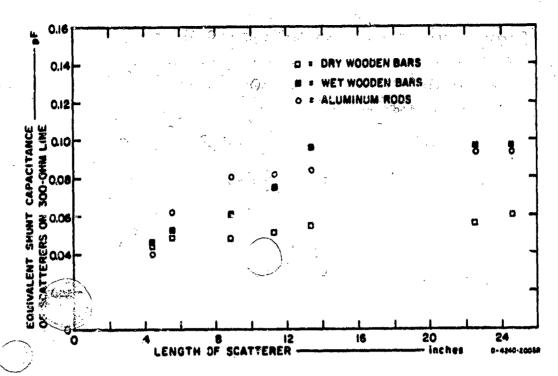


FIG. 17 MEASURED EQUIVALENT SHUNT CAPACITANCE AS A FUNCTION OF SCATTERER LENGTH

4. Effect of Electrical Properties of the Scatterer

Three types of scatterers have been used thus far: dry wood bars, wet wood bars, and aluminum rods. Some indication of the effect of conductivity can be obtained by examining the results already obtained, but it should be pointed out that the aluminum roll tree of a different shape and size than the wooden bars. Consequently we will use wooden bars of the same size and shape (but with varying water content) to study further the effect of the intrinsic complex dielectric constant of the scatterer upon the equivalent shunt admittance of the scatter are observed with our 150-ohm image-plane line at 17 MHz.

For these tests, 1-1/2-in-aquaro bars 24-1/2 in long were placed 4-3/6 in from the open end of the line. The bars were perpendicular to the line at position 19, and data were obtained with the bar two different distances from the line. Immediately after the bridge measurement the water content was determined in percent relative to the

dry weights obtained by oven drying at 60°C until the change of weight with time was negligible. The results of these tests are summarized in Table IX. An increase in equivalent shunt capacitance with increasing water content is observed. The equivalent shunt capacitance is plotted

Table IX

FQUIVALENT ADMITTANCE OF WOODEN BARS NEAR A 150-OHM IMAGE-PLANE
TRANSMISSION LINE VERSUS MOISTURE CONTENT OF BARS

		Measv≃ed		Equivalent
Water	Distance &	Equivalent	Admittance	Shunt
Content	of Scatterer	Admittance	Equivalent	Capacitance
of Bars,	to & of	of Scatterer	of Scatterer	on 300-ohm
WC	Conductor	on 150-ohm Line	on 300-ohm Line	Line
(percent)	(in)	(µmhos)	(µmhos)	(pF)
0,0	1-3/4	0.89 + 58.36	0.45 + 14.18	0.039
0.0	€	0.94 + JU.78	0,47 + j0,39	0.003
8.5	1-3/4	2.54 + j12.94	1.27 + j6.47	0,060
0.0	6	0.48 + j1.54	0.24 + 30.77	0.007
12.7	1-3/4	0.62 + j15.76	0.31 + j7.88	0.073
14.1	6	0.66 + 11.08	0.33 + 10.54	0.005
25,0	1-3/4	1.90 + j24.92	0.95 + j12.46	0.116
50.U	6	0.66 + 10.236	0.33 + j0.138	0.012
44,2	1-3/4	1.92 + j29.84	0.96 + j14.92	0.139
3, FF	6	0.44 + 13.70	0.22 + j1.85	0.017

as a function of water content in Fig. 18 for both scatterer spacings from the line conductor. The variation of effective shunt capacitance with water content is very linear for the 6-in spacing (with the exception of the value at 12.7 percent water content, which seems low), and a similar variation is apparent for the 1-3/4-in spacing. Also, values from the other tests involving wet bars have been plotted for the 1-3/4-in spacing. Dashed lines have been drawn in to illustrate these treads. These results are in agreement with those obtained with freshly cut willows in an earlier study (see Appendix of Ref. 8), where the variation of effective relative dielectric constant exhibited a linear variation with the weight (and, by inference, water content) of the willows as they dried out.

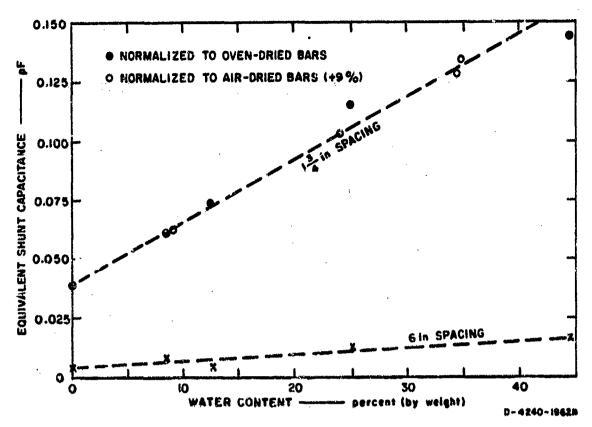
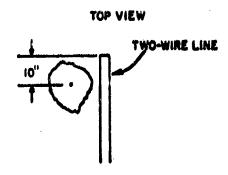


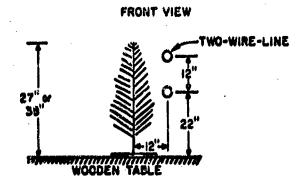
FIG. 18 EQUIVALENT SHUNT CAPACITANCE OF WOODEN BARS AS A FUNCTION OF WATER CONTENT

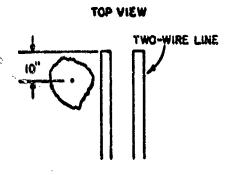
5. Equivalent Shunt Admittance of a Single Cut Pine Bough

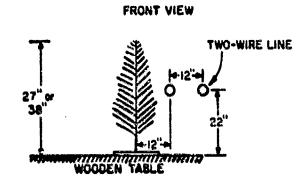
The 440-chm two-wire line was used in the laboratory to measure the equivalent shunt admittance of a single, freshly cut pine bough. The pine bough was fastened in an upright position to the wooden table used for the tests discussed in Sec. IAI-B, and data were obtained for three different configurations: line in plane parallel to table top with bough stem 12 in from nearest conductor, and line in plane perpendicular to table top (i.e., in plane parallel to bough stem) with bough stem 12 in from nearest conductor. The bough stem was always 10 in from the end of the line (between positions 17 and 16). These configurations are illustrated in the sketches in Fig. 19. The data obtained during these measurements are summarized in Table X.

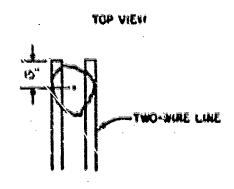












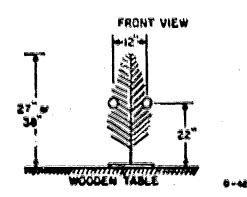


fig. 10 - Yest setup for measurements on single pine bough

Table X

EQUIVALENT SHUNT ADMITTANCE OF SINGLE PINE BOUGH

Measurement Configuration	Height of Bough (in)	Equivalent Shunt Admittance (µmhos)	Equivalent Shunt Capacitance, C (pF)	Loss Tangent
A	27	0.23 + j6.32	0.059	0.036
	38	0.92 + j9.47	0.088	0.097
В	27	0.24 + j5.21	0.048	0.046
	38	0.61 + j8.59	0.080	0.070
C	27	0.66 + 17.95	0.674	0.082

6. Equivalent Shunt Admittance of Living Oak Trees

Following the laboratory tests described in the preceding section, the 440-ohm two-conductor line was taken to the field to obtain data on a living tree. Two small cak trees (see Fig. 20) about 15 and 25 ft high (breast-height diameters about 4 in and 5-1/2 in respectively) which were conveniently located near the laboratory were selected for these tests, and the line was set up in a manner similar to that described for the tests on the cut pine boughs (see Fig. 21 for setup at the small-tree site). The results of 'bese tests are summarized in Table XI.

7. Summary of Results on Measurements of Equivalent Shunt Admittance of Single Scatterers

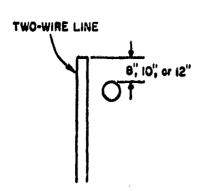
We have observed that the equivalent circuit of the single scatterer which is short relative to the wavelength of the test signal is always a lessy especitor--never an inductor. The value of the equivalent capacitance depends upon the length of the scatterer, its electrical properties (as indicated by water content in the case of weeden leatterers), its position radially from the line, and its orientation (whether the line is parallel to or perpendicular to the plane containing the scatterer). Provided the scatterer is not located in the fringing

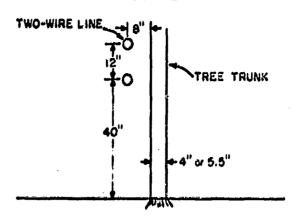




(4) 25-ft TREE

PHOTOGRAPHS OF TREES USED FOR SINGLE-TREE MEASUREMENTS EG. S

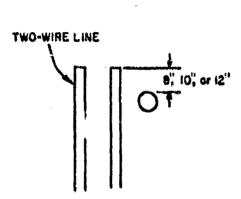


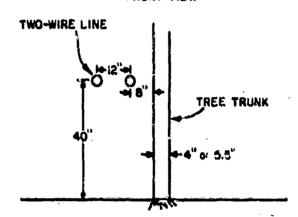


(c) MEASUREMENT CONFIGURATION A

TOP VIEW

FRONT VIEW

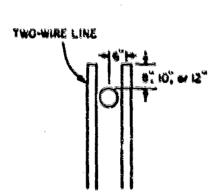


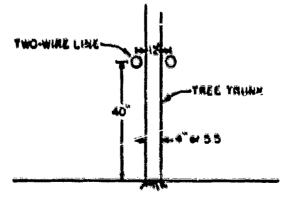


(b) MEASUREMENT CONFIGURATION B

TOP VIEW

FRONT VIEW





(c) MEASUREMENT CONFIGURATION C

FIG. 21 MEASUREMENT SETUP FOR ISOLATED-TREE TESTS

Table XI

EQUIVALENT SHUNT ADMITTANCE OF ISOLATED SWALL OAK TREES

Loss Tangent 5 = 1/wRC	0.173 0.300 0.310	0.221 0.101 0.202 0.198	0.030	0.051	0.041 0.039 0.039	0.086 0.077
Equivalent Shunt Capacitance, C (ps.)	0.065 0.100 0.101	0.097 0.119 0.118 0.121	0.079	160,0	0.088 0.093 0.095	0.120 0.125
Equivalent Shunt Admittance (umhos)	1.21 + 16.98 3.18 + 110.55 3.28 + 110.58	2.19 + 310.49 1.30 + 312.86 2.59 + 312.68 2.60 + 313.03	0.26 + 38.45	0.50 + 19.81	0.39 + 19.41 0.39 + 19.84 0.40 + 110.23	1.03 + 312.78
Distribution of Trunk from End of Line (in)	0 10 12	21 01 0	10	0.7	8 10 12	01 8
Tree Height (ft)	ខ្លួ	ន្តន្ត	51	23	15.	22
Messurement Configuration		€	Œ		į	j

fields near the open end of the line, however, the equivalent shunt admittance is relatively independent of its position longitudinally along the line. This concludes our study of the effects of single scatterers. Let us now turn our attention to the effects of more than one scatterer.

D. Mutual Impedance and Coupling Effects

In the one-dimensional model which we are using to find the equivalent dielectric constant of a distribution of scatterers we expect to neglect the mutual coupling between the scatterers and consider only the coupling of the individual scatterers to the transmission line. This coupling to the transmission line can be taken into account in the model by an equivalent shunt admittance for each scatterer. In the preceding section we have been considering this equivalent admittance and finding how it changes with various parameters which affect it. We now need to determine whether we are justified in neglecting mutual coupling effects when more than one scatterer is present or if we need to modify the equivalent circuits of the scatterers to account for mutual coupling.

Measurements were made with pairs of dry wooden bars, pairs of wet wooden bars, and pairs of aluminum rods to investigate mutual coupling effects. Two sets of measurements were made, one with the two scatterers in a plane perpendicular to both the canductors and the image plane, and the other with the two scatterers in a plane perpendicular to the image plane but parallel to the conductors. In both cases, the scatterers were perpendicular to the image plane (see Fig. 15). The results of those measurements are shown in Tables XII and XIII, respectively. Only the susceptance is given since the accuracy with which it can be determined with our measurement equipment is much better than that with which the conductance can be measured. Moreover, the con-uctance was much smaller than the susceptance and may be consider a negligible for the purpose of these tests on mutual coupling.

The results of the tests with both scatterers in a plane perpendicular to the transmission line are given in Table XII. Column 5, headed "Equivalent Shunt Susceptance," shows the measured values for

Table XII

NUTUAL COUPLING TESTS WITH SCATTERERS IN PLANE PERPENDICULAR TO 150-OHM INAGE-PLANE LINE

	Namber of		Bistance from & of		
	が自己を生物を見る		Configuration to a	Fourting Lane	
				THEFT	7
	Kassurad	Scatterer	of Scatterer	Susceptance, B Difference	Difference
Type of teatherer	Simultaneously	Postt ton	(4n)	(mayos)	(unthos)
Dry Readon Cars	H	13	1-3/4	2.6	0.0
CO DEFFERENCE MICH	***	6.	9	, cr)
34-1/12" * 1-1/2" * 1-1/2"	~	61	3-3/4 and 6	12.7	
tiet Worden Unra		61	1-3/4	25.1	5.0
(174.7 percent with	a-1	61	9	2	
24-1/2" * 1-1/2" * 1-1,2"	C4	61	1-3/4 and 6	28.6	
A summanum Mode		63	1-3/4	14.1	1.2
1/4" 413 motor & 24-1/2"	,	19	5-1/4	0.	1
	~	19	1-3/4 and 5-1/4	16.3	

See Fig. 13 for description of scatteror positions.

**
This is the difference between the susceptunce measured for the pair of scatterers and the sum of the

Table Kill

METERAL CONFILING TESTS WITH SCATTERERS IN PLANE PARALLEL TO 150-OHM IMAGE-PLANE LINE

				i		
- Same	Munition of		Bistance from t. of	Messurement		
,	SCAT ELECTE		Conductor to t		000000000000000000000000000000000000000	
-	では、一切者で	Scattorer	Of Scattoron			
The state of the s				orange and a contract of	ついにおいらいにおおいの	Difference
APPLANCE AND APPLANCE OF	A TEXT CHURCHES IN	Post Lon	(tn)	(unhos)	(capos)	
一般の はからまる 一般の	7 1	2.7	1-3/4	15.1	,	(Spinst)
CA DESTRUCT ACT	***	œ.	** C = E	• (
	i i	}	S. CTILT	4.51		
一部の一部 一部 一	* }	6	1-3/4	13.2		
	Ĉe.	17 end 18	1-3/4	0.7.	7 610	ç
	લ	18 and 19	2-3/4	4		2.
	C.		776-			1.5
	And the second s		1./C T	913.G	913.I	5,04
	4.3		1-1/8	23.8		
一般 はまかれる 本のののはない ままれ	-1	60	1-1/8	8 8 2		
	ھنب	51	1-1/8	15.6		
	**	17 and 18	1-1/8	929.1	7 4 68	
	74	18 crd 19	1-1/8	693 K		- (
	R			2 6 6 6	2,500	77.74

* See Fig. 15 for domerapsion of sestemen positions,

staticset heaver the sending and of the tipe) and the corresponding value souputed from the measured equivalent ** This is the difference between the measured susceptance of the line plus two scatterers (from the point of the each scatterer slope, and for the pair. The difference between the result for the pair and the sum of the individual susceptances is shown in Column 6. The differences are so small that they lie in the experimental error range, except possibly the result for the sluminus rod which shows a small but measurable difference.

The results of the tests with the scatterers perpendicular to the line but in a plane parallel to the line (see Table XIII) are somewhat more difficult to interpret. Here we cannot simply take the difference of the measured results for one and two scatterers to determine mutual coupling effects because the equivalent susceptance of the section of the line between the scatterers (essentially due to the capacitance per unit length for our relatively low-loss line) must be taken into account.

The measured equivalent susceptances for the individual scatterers (given in Column 5) are the values appropriate for use as lumped-constant equivalents at the position of the scatterer down the line. The measured equivalent susceptances for the pairs of scatterers represent the lumped-circuit equivalent of the line plus scatterers as seen at the scatterer closer to the sending end of the line looking toward the load end of the line (which was an open circuit for these tests). The value of equivalent susceptance seen at this point was computed for the case of two scatturers from the measured values for the individual scatterers under the assumptions of no entual coupling and a perfectly conducting line. Therefore, the difference between this computed value and the observed value with both scatterers present is a measure of the mutual effect. Unfortunately, the line susceptance is much greater than the susceptance of any individual scatterer and we must rely upon the difference of two large numbers for our estimate of the mutual effect.

For the aluminum rods this difference is about 10 percent of the value of the susceptances of the individual statterers and it may be reactuated that mutual coupling is negligible in this case. Indeed, the observed differences are near the limit of the accuracy of our measurements. For the wooden here, the nutual effect is significant when the bare are in adjacent positions as expected, but the offect appears

negligible when the bars are separated by only one position. Perhaps the increase in the magnitude of the apparent sutual coupling of the wood bars over that of the aluminum rods when the scatterers are in adjacent positions may be explained in part by the larger size of the bars which, for a fixed spacing (see Fig. 15), places the bars physically closer together. The separation of the wooden bars in adjacent positions (all/240 at 17 MHz) is only about twice the width of a single bar, whereas the separation of the aluminum rods in adjacent positions is about sixteen times the diameter of a single rod.

The results of those messurements of his pairs of scatterers appear to justify the assumption that the wild coupling is negligible in most practical cases (i.e., excep together), and that the principal wild is the coupling of the individual scatterers to the transmiss. I line.

E. Many Scatterers Randowly Distributed about a Transmission Line

1. Methods of Approach

Our objective was to determine the feasibility of representing a forest as a dielectric medium and of measuring the dielectric properties of this medium by weens of tropsplasion-line probes. We have elreddy discussed the effect of individual scatterers and have concluded that each scatterer of any of the shapes and sizes (short compared to the wavelength of the test signal) investigated could be represented by a stupt capacitiance with an associated stunt conductance pluced across the transmission line at the position of the scatterer. We now need to consider the case of many scatterers randomly distributed about the transmission like, as trees in a forest would be, and see whether we can represent a region with hear discrete scatterers as if it were filled . with a coatipuous medium characteries. By a dislectric comptant with associated less factors. In other words, we are coloc to make a model of the forest using wooder bars or netal cylinders as trees and determine the effective dielectric constant of the model by means of a transmission line probe.

In carrying out this part of the investigation we approached the problem in each of two ways. First, we placed scatterers randomly about the transmission line, relling dice to see whether or not a "tree" should be at each position of a two-dimensional grid. We then measured the input impedance of the line with the termination open circuited and again with the termination short circuited, and (using the equations of Sec. II) calculated the effective dielectric constant, permeability and loss targent. This process was repeated five times (see Fig. 22 for the actual scatterer positions used) and the results were averaged. These average values are termed measured values. Our second approach to the

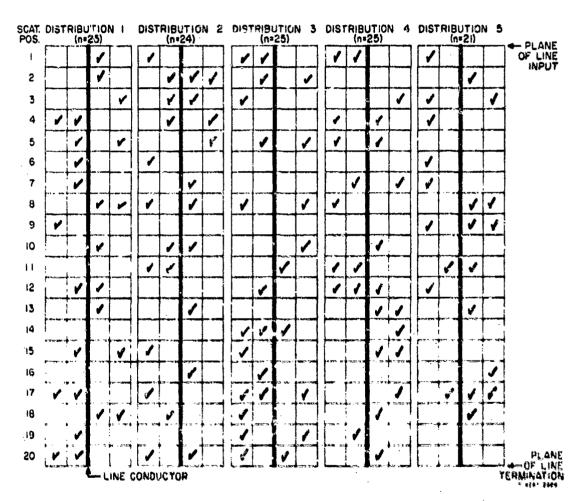


FIG. 22 RANDOM DISTRIBUTIONS OF SCATTERERS USED FOR MEASUREMENTS

1

multiple-scatterer problem was based on previous measurements, but it involved computation only. In the latter case, we constructed a distribution of sizes of lossy capacitors from the measured results for single scatterers and used a random-number generator to decide what size capacitor to place at each of the uniformly spaced intervals along a hypothetical transmission line. We then calculated the input impedance of the hypothetical line when open and short circuited and again used the equations of Sec. II to convert to the electrical parameters of the medium around the line. The process was repeated ten times, and average values, which we call calculated values, were obtained. The remainder of this section will deal with a comparison of such measured and calculated values for various example cases.

2. 17-MHz Tests with Image-Plane Line

Tests were made with the $\lambda/8$ image-plane line on the dry wood (9 percent WC) and wet wood bars (≈ 25 percent WC) and aluminum rods used in the early or vets. For these tests the scatterers were set up perpendicular to the image plane. The details of the line spacing and the scatterer spacings are pictured as insets on the figures showing the calculated and measured values.

a. Dry Wood Bars

For the first tests on the dry wood bars, the center of the transmission-line conductor was positioned 4.6 in above the aluminum plate which forms the image plane. The measured values are summarized in Table XIV and the calculated values are given in Table XV. The average values of the real parts of the relative complex dielectric constant and complex permeability are plotted as a function of the number of scatterers (i.e., scatterers per wavelength) in Fig. 23.

The conductor then was lowered so that its center was 1.452 in above the aluminum plats and measurements were repeated. Tables XVI and XVII summarize these results: the average values of the real parts of the complex relative dielectric constant and permeability are plotted in Fig. 34 as a function of the number of scatterers.

Table XIV

ELECTRICAL CONSTANTS WITH DRY WOOD BARS MEASURED

WITH 200-OHM IMAGE-PLANE LINE

Random Distribution Number	Number of Scatterers n	Relative Dielectric Constant t	Relative Permeability $\mu_r = \mu_r - j\mu_r$	Loss Tangent
1	25	1.080	0.994 - j0.002	0.0082
2	24	1.090	0.990 - 30.000	0.0079
3	25	1,057	0.994 - 10.002	9.0055
4	. 25	1.076	0.997 - 10.003	0.0062
5	21	1,063	0,994 - 10,000	0.0062
Average	24	1.080	0.9 94 - j0.001	0.0068

TABLE YV

ELECTRICAL CONSTANTS WITH DRY WOOD BARS CALCULATED
FOR 200-OHN IMAGE-PLANE LINE

Number of Scatterers n	Relative Dielectric Constant	Relative Permeability	Loss Tengent Š
10	1.040	1,001 - 19,000	0,0023
20	1.060	1.031 - 10.000	0.00451
25	1,084	1.006 - 10.000	მ ,6მეენ
30	1.114	690, Ut ← C00. I	0,0067

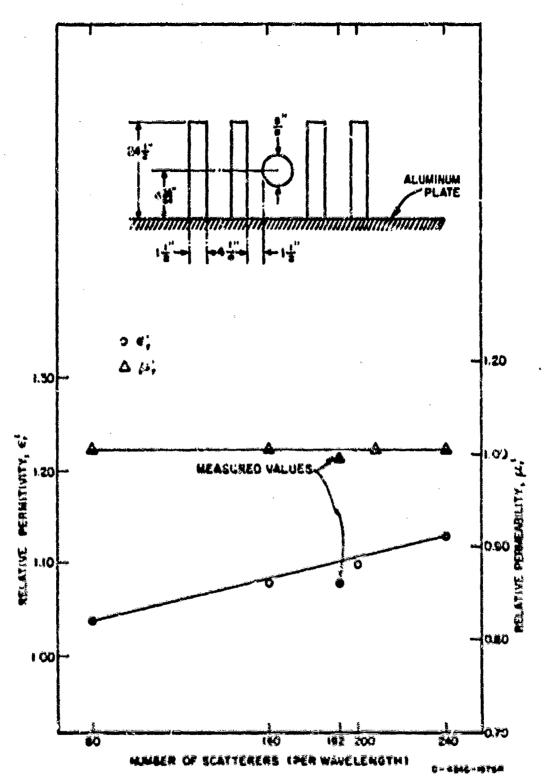


FIG. 2) EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING DRY WOOD BARR--CALCULATED AND MEASURED WITH 200-0mm (MAGE-PLANE LINE

Table XVI

ELECTRICAL CONSTANTS WITH DRY WOOD BARS MEASURED

WITH 135-OHM IMAGE-PLANE LINE

Random Distribution Number	Number of Scatterors	Relative Dielectric Constant e'r	Relative Permeability $\mu_r = \mu_r - j\mu_r$	Loss Tangent
1	25	1.039	1.016 - 10.002	0.0011
2	24	1.059	1.016 - 10.001	0,0025
3	25	1,038	1.020 - 10.002	0.0014
4	25	1.030	1,026 - 10,003	0,0015
5	21	1.034	1.016 - 30.001	6.0025
Average	24	1.041	1.019 - j0.002	0.0018

Table XVII

ELECTRICAL COSSTANTS WITH DRY WOOD BARS CALCULATED
FOR 135-ORN IMAGE-PLANE LINE

Number of Scatterers n	Roletive Dielectric Constant t	Relative vermeability $\mu_{r} = \mu_{r} - J \mu_{r}^{\prime}$	Loss Tengant
10	1,021	1,000 - 10,000	0.0049
20	1.045	1,002 - 10,000	0.010
25	¥20. 1	1,001 - <u>1</u> 0,000	0.013
30	1,066	1.000 - 10.000	0.015

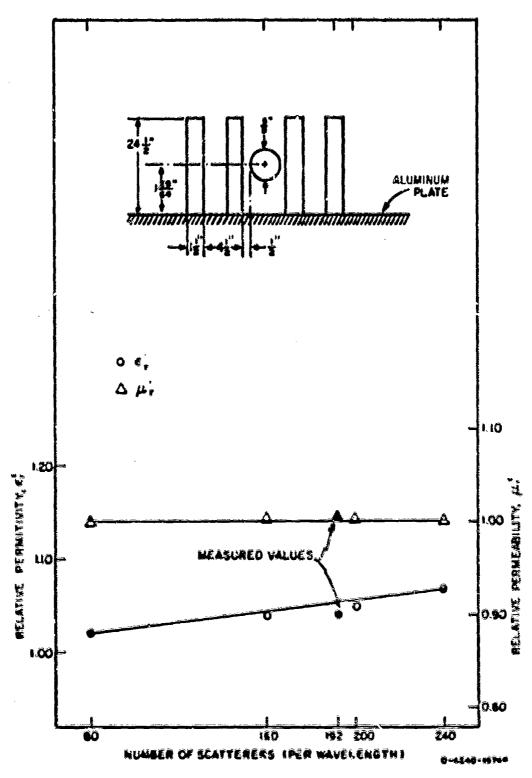


FIG. 24 EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING DRY WOOD BARS--CALCULATED AND MEASURED WITH 335-04m MAGE-PLANE LINE

b. Wet Wood Bars

Wet bars (moisture content 20 percent by weight) were used as scatterers with the center of the transmission-line conductor at 1.375 in above the aluminum plate. Data were obtained with both 80 and 160 scatterers per wavelength; the results are summarized in Table XVIII (measured values) and in Table XIX (calculated values). These data are plotted in Fig. 25.

Teble XVIII

ELECTRICAL CONSTANTS WITH WET WOOD BARS MEASURED
WITH 150-OHM IMAGE-PLANE LINE

Random Distribution Number	Number of Scatterers	Relative Dielectric Constant	Relative Permeability \(\mu_r = \mu_r - \mu_r \)	Loss Tangent &
1	10	1.064	0.992 - 10.002	0.009
1	20	1.111	0.992 - 30.002	0 012
2	10	1.077	0.997 - 10.002	0.012
2	20	1.099	0.997 ~ 50.002	0.010
3	10	1.062	0.969 + 10.001	0.011
3	20	1,111	160.01 + 686.0	0.009
ů.	10	1.047	0.966 + 10.000	0.010
4	20	1.119	0.966 + 10.000	110, 6
5	10	1 .079	0,990 • 10,000	0.016
5	20	1,157	060.0t • 088.0	0.012
Average	10 20	1,066 1,115	000,0t = 000,00 000,0t = 000,0	0.011 0.011

e. Metal Rods

For the first of these tests, the center of the conductor was placed 1.575 to above the aluminum place, the 1/8-in-diameter aluminum rada were positional perpendicular to the aluminum plate. The

Table XIX

ELECTRICAL CONSTANTS WITH WET WOOD BARS CALCULATED
FOR 150-OHM IMAGE-PLANE LINE

Number of Scatterers n	Relative Dielectric Constant e' _r	Relative Permeability $\mu_{r} = \mu_{r}' - j\mu_{r}''$	Loss Tangent
20	1.075	1.000 - 10.000	0.910
20	1.136	1.000 - 10.000	0,017

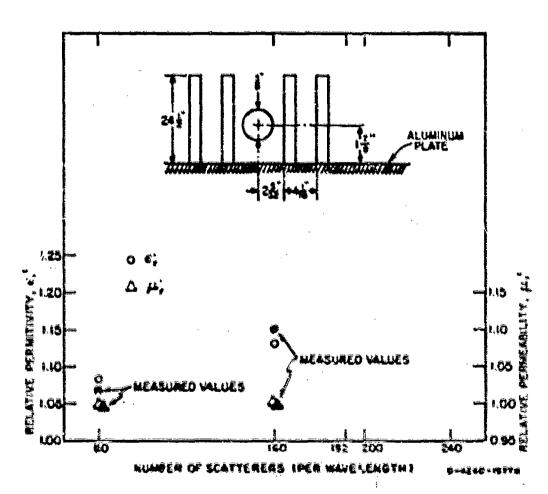


FIG. 25 EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING WET WOOD BARS--CALCULATED AND NEASURED WITH 150-64m MAGE-PLANE LINE

results are summarized in Table XX (measured values) and in Table XXI (calculated values). Figure 26 shows these results along with a sketch of the measurement satup.

Table XX

ELECTRICAL CONSTANTS WITH METAL RODS PERPENDICULAR T/V ZERO-POTENTIAL

PLANE MEASURED WITH 150-OHM IMAGE-PLANE LINE

Raudom Distribution Number	Number of Scatterers n	Relative Dielectric Constant	Relatice Permesbility $\mu_{\mathbf{r}} = \mu_{\mathbf{r}}' - j \mu_{\mathbf{r}}''$	Aoss Tangent 6
1	25	1,197	1.101 - 10.0034	0,00256
2	24	1.165	1.100 - 10.0037	V.00283
3	25	1.171	1.104 - 10.1022	0.00249
4	25	1.148	1.107 - 10.0024	0.00071
5	21	1.160	1.100 - J0.0020	0.00267
Averege	24	1.168	1.105 - jr.0028	0.00285

Table XXI

ELECTRO-L CONSTANTS WITH METAL HORS PERPENDICULAR TO ZERO-POTENTIAL

PLANE CALCULATED FOR 150-SEM IMAGE-PLANE LINE

Number of Scatterers	Kolutive Diolectric Commissiont c	Relative Personability	Loss Tengant
10	1.046	1,001 = j0,001	0,60264
20	1,095	1,002 - 30,004	0,00576
25	* 1.111	1,001 = 30,63	0.63631
30	1,142	1.003 = 10.000	0.00825

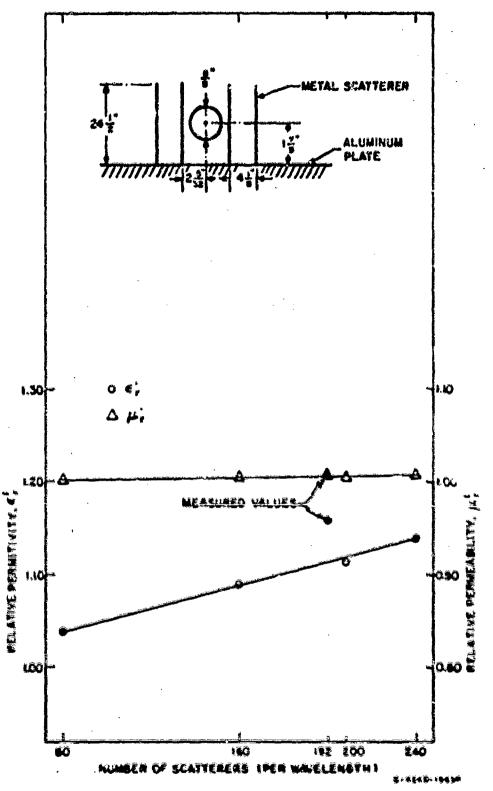


FIG. 20 EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING METAL ROOS PERPENDICULAR TO ALUMINUM PLATE--CALCULATED AND MEASURED WITH 180-one IMAGE-PLANE LINE

These tests were repeated with the aluminum rods parallel to the aluminum plate but still perpendicular to the transmission-line conductor (which remained at 1.875 in above the aluminum plate). Tables XXII and XXIII summarize the measured and calculated results respectively, and Fig. 27 shows the average values of the real part of the complex relative dielectric constant and permeability as a function of the number of scatterers per wavelength.

Table XXII

ELECTRICAL CONSTANTS WITH METAL RODS PARALLEL TO IMAGE PLANE
WEASURED WITH 150-OHM IMAGE-PLANE LINE

Random Distribution Number	Number of Scatterers n	Relative Dielectric Constant er	Relative Permeability $\mu_{p} = \mu_{r} - J\mu_{r}$	Loss Tangent
1	25	1.064	0.978 - 10.001	0.0025
2	24	1.057	0.974 - 10.001	0.0025
3	25	1.071	100.01 - Eee.0	0.0025
4	25	1.667	0.994 - 10.002	0.0021
5	21	1.075	1.008 - 10.002	0.0023
Average	24	.066	0.990 - 10.601	0.0024

TADIS XXIII

ELECTRICAL CONSTAN^{AMOS} WITH METAL ROOS PARALLEL TO IMAGE PLANE

CALCU A MAR POR 150-ONE IMAGE-PLANE LINE

Yumber of Scatterers n	Relative Jielcetrie Commissi (*	Relative Personality	Loss Tragent
19	1.017	1,0005 - 30,000	0.00,55
20	1.338	1.002 = 100.00	66160.0
25.	1,650	0:00.00 - 100.00	0,00255
3ô) .O\$3 ·	1,602 - 30,60	0.00283

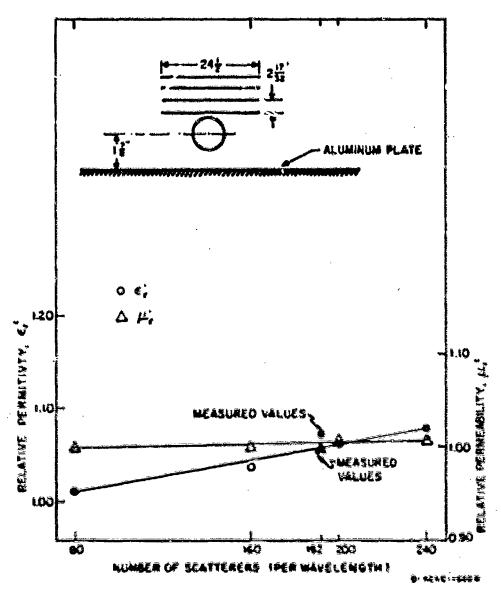


FIG. 27 EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING METAL ROOS
PARALLEL TO ALUMINUM PLATE -- CALCULATED AND MEASURED WITH 150-044
MAGE-PLANE LINE

3, 17-MHz Tests with 300-Ohm Two-Conductor Line

Tests also were made with the $\lambda/8$ two-conductor line on the dry wood, wet wood, and aluminum rod scatterers. For these tests the scatterers were positioned perpendicular to the line as shown on the inserts on the figures showing the calculated and measured results.

a. Dry Wood Bars

The measured and calculated values are summarized in Tables XXIV and XXV. The average values of the real parts of the complex relative dielectric constant and permeability are shown in Fig. 28 as a function of the number of scatterers per wavelength.

Table XXIV

ELECTRICAL CONSTANTS WITH DRY WOOD BARS MEASURED
WITH 300-OHN TWO-WIRE LINE

Rendom Distribution Number	Number of Scatterers n	Rolative Dielectric Constent	Relative Peresability Fr = Fr - JFr	Loss Tengent
1	25	1,074	0.987 - 10.013	810.0
2	24	1.059	0,992 - 10.613	0.016
3	25	1,101	0,975 - 30,012	0.017
4	25	1,060	0.984 · 90.013	0.017
5		1.051	0.998 - J0.015	710,0
Averege	24		810, Qt - 0 9 9, 0	0.017

b. Wet Wred Bars

The measured and extruisted values for the bars with 15 percent water content by weight are summerized in Tables ARVI and ARVII respectively. The average values of the real pert of the complex relative dielectric constant and persesbility are shown in Fig. 29 as a function of the number of meathers not vavelingth. Values are also

Table XXV

ELECTRICAL CONSTANTS WITH DRY WOOD TABLE CALCULATED
FOR 300-DRM TABLE LINE

Number of Scatterers n	Rolative Dielectric Constant e'r	Relative Pormosbility	Loss Tengent
10	1.011	1.004 - 10.000	0.0035
20	1.03€	1.000 - 10.000	0.007
25	1.060	1.003 - 10.000	0.009
30	1,079	1.000 - 10.000	0.010

shown on Fig. 29 for bars with 8 percent water content for the case of . 160 scatterers per wavelength.

c. Metal Rods

Measured and calculated values are summarized in Tables XXVIII and XXIX. The average values of the real parts of the complex relative dielectric constant and permeability are shown in Fig. 30 as a function of the number of scatterers per wavelength.

e. Discussion of Results of Laboratory Multiple-Scatterer Tests

of the effective rowies relative dielectric constant and complex relative permeability of the region filled with acutterers calculated on the basis of representing the short scatterers as effective lossy sheat capacitances on the transmission line and the average values actually measured with the lines in the laboratory. This agreement further encourages us to consider estimating these quantities for an actual forest from forest measuration data (i.e., distribution of tree sizes and number of trees per unit area or searest-neighbor distance data) together with the measural effect of a single tree (i.e., scatterer). Such forest measuration data are available for selected forests in The shand. The would remain only to determine by measurement the equivalent current of

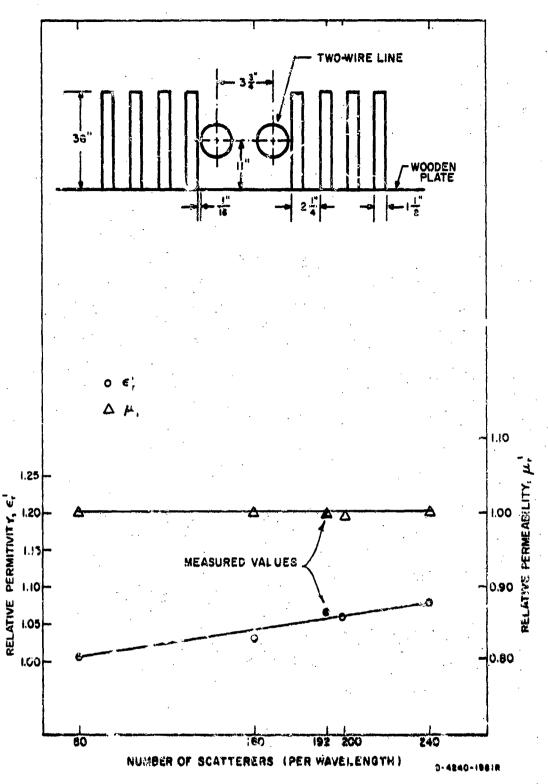


FIG. 28 EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING DRY WOOD BARS--CALCULATED AND MEASURED WITH 300-ohin TWO-WIRE LINE

Table XXVI

ELECTRICAL CONSTANTS WITH WET (15 PERCENT WC) WOOD BARS

MEASURED WITH 300-OHM TWO-WIRE LINE

Random Distribution Eumber	Number of Scatterers	Relative Dielectric Constant	Relative Permeability $\mu_{\mathbf{r}} = \mu_{\mathbf{r}}' - j\mu_{\mathbf{r}}'$	Loss Tangent
1	25	1,105	1.000 - 40.011	0,025
- 2	. 24	1.090	0.998 - J0.011	0.032
3	25	1,118	0.988 - JO.015	0.028
4.	25	1,120	1.012 - 10.015	0,028
5 -	21	1,099	1.009 - JO.014	0.025
Average	24	1.107	1.000 - 50.013	0.025

Table XXVII

ELECTRICAL CONSTANTS WITH WET (15 PERCENT WC) WOOD BARS

CALCULATED FOR 300-OHM TWO-WIRE LINE

Number of Scatterers n	Relative Dielectric Constant & r	Relative Permeability $\mu_{\mathbf{r}} = \mu_{\mathbf{r}}' - \mathbf{j}\mu_{\mathbf{r}}''$	Loss Tangent
10	1.040	1.003 - j0.000	0.006
20	1.079	0.999 - 30.000	0.012
25	1.110	1,605 - 30,000	0.017
30	1,171	1.000 - j0.000	0.019

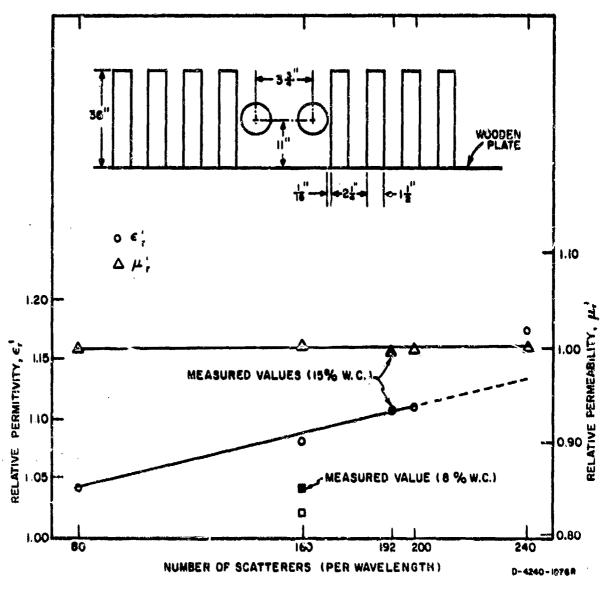


FIG. 29 EFFECTIVE ELECTRICAL CONSTANTS OF VOLUME CONTAINING WET WOOD BARS--CALCULATED AND MEASURED WITH 300-ohm TWO-WIRE LINE

Table XXVIII

ELECTRICAL CONSTANTS WITH METAL RODS MEASURED
WITH 300-OHM TWO-WIRE LINE

Random Distribution Number	Number of Scatterers n	Relative Dielectric Constant E'r	Relative Permeability Spr = Mpr - jMpr	Loss Tangent 8
1	25	1.064	0.999 - j0.013	0.015
2	24	1.063	0. 992 - j0.012	0.015
3	25	1.081	0.997 - j0.013	0.015
4	25	1.061	1.004 - j0.013	0.015
5	21	1,098	0.992 - j0.012	0.016
Average	24	1.073	0.997 - J0.013	0.016

Table XXIX

ELECTRICAL CONSTANTS WITH METAL RODS CALCULATED

FOR 300-OHM TWO-WIRE LINE

Number of Scatterers n	Relative Dielectric Constant $\epsilon_{ m r}'$	Relative Permeability $\mu_{\mathbf{r}} = \mu_{\mathbf{r}}' - j\mu_{\mathbf{r}}''$	Loss Tangent
10	1.027	1.002 - j0.000	0.002
20	1.057	000.0t - 866.0	0.005
25	1,064	3.001 - JO.000	0.006
30	1 .082	1,004 - j0.000	0.006

the trees as a function of tree size, shape, and distance from the line of interest (such as was done for the oak trees in Sec. V-C-6) in order to generate the required set of equivalent lossy capacitors. These equivalent circuits could then be used, along with the technique reconstituted above, to calculate the effective electrical proporties of the forest considered as a lossy disjectric slab. These values could then

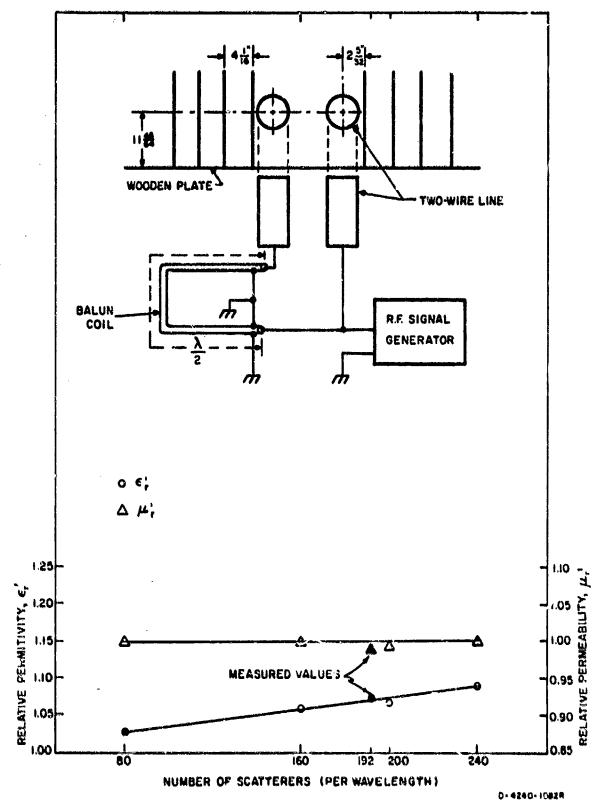


FIG. 30 EFFECTIVE ELECTRICAL CONST. ITS OF VOLUME CONTAINING METAL RODS--CALCULATED AND MEASURED WITH 300-Lhm TWO-WIRE LINE

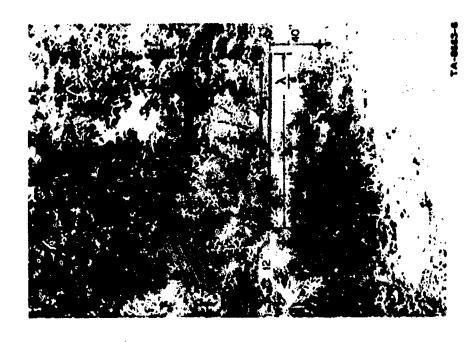
be compared with actual values of the slab constants as determined by open-wire transmission-line measurement. This technique is illustrated in Sec. VI.

5. Results of Measurements with Transmission Lines in Living Vegetation in South Carolina

Data already have been taken under this contract with transmission lines in forests in the western part of the U.S.^{8,9,10} and in Thailand.^{11,12,13} The purpose of this section is to present and discuss some results obtained more recently in living vegetation in South Carolina.

The $\lambda/8$ two-conductor line was used in clumps of small pines (see Figs. 31 and 32) and camellia bushes (see Fig. 33) to measure at 17 MHz the relative dielectric constant, loss tangent, and complex relative permeability of the volume containing the living vegetation. The data (see Table XXX) were obtained with a 440-ohm line (5/8-in conductor diameter and 12-in spacing) on a cool (48°F), cloudy spring day. The relative humidity was 75 percent. Two line orientations were used: plane of line parallel to ground and plane of line perpendicular to ground.

The values of complex dielectric constant obtained with the line parallel to the ground compare with typical values obtained in the carlier forest measurements reported in Refs. 8 and 13. It may be noted that the values of the real part of the complex dielectric constant obtained with the line perpendicular to the ground are somewhat higher than the values obtained with the line parallel to the ground, indicating that the vegetation is anisotropic as observed with the line. This is in contrast to earlier results where the line orientation produced essentially similar results, and also in conflict with the study on anisotropy presented in Sec. IV of this report. Presumably this apparent observed anisotropy in e_r' results from the small number of samples averaged to give the values shown in Table XXX. The observed values for the less tangent appear more isotropic—as expected for a line with R_c as high as 440 ohms (see Fig. 13)—whereas the setual values of less tangent in forests probably are anisotropic. • ,8,28





74





FIG. 32 TEM-ft PINE TREES AND APPROXIMATE LINE POSITION





FIG. 33 TEN-II CAMELLIA TREES AND APPROXIMATE LINE POSITION

Table XXX

PIELD MEASUREMENT OF ACTUAL POREST EFFECTIVE ELECTRICAL PROPERTIES WITH 440-OHM TWO-WIRE LINE (A/8) AT 17 MHz IN SOUTH CAROLINA

Type of Porest	Verage Huight of Tree (ft)	Average Number of Trees per Acre	Orientation of Two-Wire Line	Distance of Line from Ground (ft)	Relative Dielectric Constant	Relative Permeability L = L = Jur	Loss Tangent at 17 MHz
Cancl 1 ta	6	000	plane of two-	m	1.084	1.063 - 30.002	0.03
2110	IJ	309 9	etre line carallel to	n	1.051	1.008 - 30.063	0.
Pine	10	8.90	graups	က	1.071	1.035 - 30.003	0.03
Camell ta	8,	00.7	plane of two-	***	1.12	1.002 - 30.002	90.0
Pine	13	000	perpendicular	.	1.07	1.000 + 10.002	0.0
Pirc	0.7	800	to ground	2	1.14	0.890 - 10.002	0.03

This discussos was geneured from the lower canductor to ground.

The observed valurs of relative permeability also agree reasonably well with previous observations. The one observad value of ω_{p}' in Table XXX less than one may be considered unity to within the accuracy of the measurement (see also Appendix E for a discussion of Reasurement errors coused by incomplete spatial sampling such as avoiding the placement of a tree trunk at the OWL input).

VI CONCLUSIONS AND RECOMMENDATIONS

A. Conclusions

- (1) It was determined theoretically and verified experimentally that the maximum effective sensing volume for a 300-ohm line is a cylinder (of radius approximately 1-1/2 times the line spacing) placed symmetrically around the line and approximately the length of the line. Of course, the region of greatest sensitivity is nearest the conductors in the vicinity of voltage maxima.
- (2) Open wire lines (OWL's), except possibly very low-impedance lines ($R_{\rm C} < 100$ obms), are not very useful in resolving anisotropy of the medium into which the line is inserted.
- (3) Single scatterers such as trees near an OWL may be modeled as lossy shunt capacitors. The expectance is a function of the geometry (i.e., tree size, shape, and proximity to the line). The measurements of equivalent shunt conductance were not as accurate as the capacitance measurements, but the limited results obtained indicate that the loss tangent of the equivalent capacitor is relatively insonsitive to acatterer position. These results on the effects of scatterers are important regarding the theory of RF transmission lines passing near trees as well as for the modeling of wave propagation in forests.
- (4) A forest can be considered to consist of an ensemble of such scatterers distributed along the transmission

The concept of a seasing radius or volume is imprecise, but hevertheless it is of some usessimess in visualizing how the line samples the electrical properties of a vegetated region

line. When the equivalent circuit of a single scatterer (tree) as a function of the geometry is known and when the distribution of tree sizes and shapes is known for a given forest, then these date can be used to compute the effective macroscopic electric constants for a forest considered as a lossy dielectric slab.

(5) Therefore, OWL probes are useful for estimating the macroscopic electrical properties of a volume containing living vegetation--even when significant scatterers (e.g., tree trunks) are present--although the results of OWL measurements must be interpreted with care in this latter case and in other cases where emisstropy may be significant.

B. Reconsendations

Corclusions (4) and (5) should be checked by experiment as follows:

- ()) The statistical distribution of tree heights, diameters and spacings should be determined for a given forest.
- (2) The equivalent circuits for representative excepts trees of this forest should be necessarily as a function of presentity to se ONL (or ONL's).
- (3) The effective macroscopic electric constants for the slab should be calculated for many cases using the random program discussed in Sec. I and an estimate of the actual slab properties inferred from an average of these results.
- (!) These constants about then be used in a forest-elab model to predict extense height-gain and path-loss functions.

- (5) Then, an OWL probe should be used to measure the effective slab constants in the actual forest and a comparison made with the average values computed using the random program.
- (6) The height-gain and path-loss functions should be recalculated using electrical constants computed from the octual ONL measurements.
- (7) The height-main and path-loss functions then should be measured and compared with those calculated using both inferred and measured also constants.

If the suggested comparisons prove successfut, then a significent step will have been taken toward relating the type of forest descriptions currently being made by environmental actentiats to the needs of researchers in the field of radio propagation and communication.

Appendix A

DERIVATION OF RELATIVE POWER DENSITY

Appendix A

DERIVATION OF RELATIVE POWER DENSITY

For a TEM wave, the power density S is given by

$$S = K(\nabla \varphi)^2$$

where K is a constant, ϕ is a scalar potential function satisfying

$$\nabla^2 \varphi = 0$$

and

$$\frac{\partial \omega}{\partial \omega} = 0$$

on the surface S of the conductors.

In order to find the power density around the open two-wire line, we first consider the power density in the region between the conductors of a coaxial line.

Using polar coordinates r and 9, we have

$$\nabla^2 v = \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \phi}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 \phi}{\partial \theta^2} = 0$$

Because of symmetry, ψ is independent of θ . The above equation reduces to

$$\frac{1}{r}\frac{d}{dr}\left(r\frac{d\varphi}{dr}\right)=0$$

$$\mathbf{r} \frac{\mathrm{d} \phi}{\mathrm{d} \mathbf{r}} = \mathbf{C}$$

where C and D are constants.

Preceding page blank

Since the boundary of the conductors is defined by ${\bf r}$ = 8 and ${\bf r}$ = b, the condition

$$\frac{\partial S}{\partial \phi} = 0$$

on the surface S of the conductors was satisfied automatically when we chose ϕ to be a function of r only.

$$(\nabla \varphi)^{2} = 7\alpha \cdot \nabla \varphi$$

$$= \hat{\mathbf{r}} \cdot \frac{\mathbf{c}}{\mathbf{r}} \cdot \hat{\mathbf{r}} \cdot \frac{\mathbf{c}}{\mathbf{r}}$$

$$= \frac{\mathbf{c}^{2}}{2} \quad .$$

The power density S becomes

$$S = K(\nabla_{\Theta})^{2}$$

$$= \frac{KC^{2}}{r^{2}}$$

$$= \frac{A}{r^{2}}$$

where $r^2 = u^2 + v^2$, and u, v are rectangular coordinates.

The total power flowing down the line is

$$P_{o} = 2\pi \int_{P_{o}}^{1} P(u,v) r dr$$

$$= 2\pi A \ln \left(\frac{1}{r_o}\right) \qquad .$$

We normalize S so that

$$P = \frac{S}{P_0}$$

where P is the normalized power density; then

$$P = \frac{1}{2\pi \ln \left(\frac{1}{r_0}\right)} \cdot \frac{1}{r^2}$$

$$= \frac{B}{r^2}$$

where

$$B = \frac{1}{2\pi \ln \left(\frac{1}{r_0}\right)}$$

But the characteristic impedance of the coaxial line is

$$R_{c \text{ coax}} = \frac{\zeta}{2\pi} \ln \left(\frac{1}{r_o} \right)$$

and that of the open two-wire line is known to be

$$R_{c1w} = 2 R_{c cc}$$

B is therefore given by

$$B = \frac{\zeta}{2\pi^2 R_{\text{cTW}}}$$

Now under the transformation to the coaxial line given by

$$W = \frac{Z - 1}{Z + 1}$$

where $W \approx u + iv$, $Z \approx x + iy$, the power density p(x,y) in z-plane is related to p(u,v) in w-plane by (see Appendix B)

$$p(x,y) = \left(\frac{\eta_{xy}v}{\delta x}\right)^2 p(u+v)$$

$$= \left[\left(\frac{\partial v}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial y}\right)^2\right] + \frac{B}{u^2 + v^2}$$

From the transformation we defined, we have

$$u = \frac{x^2 + y^2 - 1}{(x + 1)^2 + y^2}$$
$$v = \frac{2y}{(x + 1)^2 + y^2}$$

Substituting in the above expression for p(x,y), we have

$$p(x,y) = \frac{4B}{(x^2 + y^2 - 1)^2 + 4y^2}$$

For a contour of constant power density, let

$$p(x,y) = p_k$$

and

$$D^2 = \frac{4B}{p_k} \qquad .$$

Then,

$$(x^2 + y^2 - 1)^2 + 4y^2 = D^2$$

At x = 0, y = 0, we have

$$p_k = 4B$$

and

$$D = 1$$

So, if we take D=1 contour as O-dB contour, then the power in dB based on D=1 contour as reference is given by

$$p = 10 \log_{10} \frac{1}{D}$$

Appendix B

EQUIVALENCE OF POWER FLOW IN THE COMPLEX z AND w PLANES

Appendix B

EQUIVALENCE OF POWER FLOW IN THE COMPLEX z AND w PLANES

It is known that for the TEM wave, the power density S is proportional to $\left(\nabla\phi\right)^2$, that is,

$$S = K(\nabla \omega)^2$$

where K is a constant, ϕ is a scalar potential function satisfying

$$\nabla^2 \varphi = 0$$

and

$$\frac{\partial \varphi}{\partial S} = 0$$

on the surface S of the conductors. Let the mapping Z = F(w), where z = x + iy, and w = u + iv, be conformal; then Cauchy-Riemann equations apply; that is,

$$\frac{\partial x}{\partial u} = \frac{\partial y}{\partial v}$$

and

$$\frac{\partial v}{\partial x} = -\frac{\partial u}{\partial y} \qquad .$$

The equations for metric coefficients are known to be

$$\frac{\partial}{\partial u} = \frac{\partial}{\partial v}u$$

$$= \frac{\partial x}{\partial u} \frac{\partial x}{\partial v} + \frac{\partial y}{\partial u} \frac{\partial y}{\partial v}$$

$$= \frac{\partial x}{\partial u} \frac{\partial x}{\partial v} - \frac{\partial x}{\partial u} \frac{\partial x}{\partial v}$$

= 0

$$\hat{\sigma}_{uu} = \left(\frac{\partial x}{\partial u}\right)^2 + \left(\frac{\partial y}{\partial u}\right)^2$$
$$= \left(\frac{\partial x}{\partial v}\right)^2 + \left(\frac{\partial y}{\partial v}\right)^2$$
$$= \partial vv \qquad .$$

The gradient of ϕ is therefore given by

$$\nabla \varphi = \hat{x} \frac{\partial \varphi}{\partial x} + \hat{y} \frac{\partial \varphi}{\partial y}$$

$$= \frac{\hat{u}}{\left(\partial_{uu}\right)^{1/2}} \left[\hat{u} \frac{\partial \varphi}{\partial u} + \hat{v} \frac{\partial \varphi}{\partial v}\right]$$

$$= \frac{1}{\left(\partial_{uu}\right)^{1/2}} \left[\hat{u} \frac{\partial \varphi}{\partial u} + \hat{v} \frac{\partial \varphi}{\partial v}\right]$$

and

$$* \frac{1}{\partial u} \left[\left(\frac{\partial u}{\partial v} \right)^2 * \left(\frac{\partial u}{\partial v} \right)^2 \right]$$

$$* \frac{1}{\partial u} \left[\left(\frac{\partial u}{\partial v} \right)^2 * \left(\frac{\partial u}{\partial v} \right)^2 \right]$$

So we hade

$$\left(\frac{\pi}{2} \nabla_{\varphi}\right)^{2} = \frac{1}{2} \left(\frac{\pi}{2} \nabla_{\varphi}\right)^{2}$$

under the conformal mapping,

The relation between the area element dA in the z-plane and dA uv in the w-plane is found to be

$$\frac{\partial u}{\partial x} = \left(\frac{\partial x}{\partial x}\right)^2 + \left(\frac{\partial y}{\partial y}\right)^2 \\
\frac{\partial u}{\partial x} = \left(\frac{\partial u}{\partial x}\right)^2 + \left(\frac{\partial u}{\partial y}\right)^2$$

The gradient of ϕ is therefore given by

$$\nabla \varphi = \hat{x} \frac{\partial \varphi}{\partial x} + \hat{y} \frac{\partial \varphi}{\partial y}$$

$$= \frac{\hat{u}}{\left(\partial_{uu}\right)^{1/2}} \frac{\partial \varphi}{\partial u} + \frac{\hat{v}}{\left(\partial_{uu}\right)^{1/2}} \frac{\partial \varphi}{\partial v}$$

$$= \frac{1}{\left(\partial_{uu}\right)^{1/2}} \left[\hat{u} \frac{\partial \varphi}{\partial u} + \hat{v} \frac{\partial \varphi}{\partial v} \right]$$

and

$$(\nabla \varphi)^{2} = \nabla \varphi + \nabla \varphi$$

$$= \left(\frac{\partial \varphi}{\partial x}\right)^{2} + \left(\frac{\partial \varphi}{\partial y}\right)^{2}$$

$$= \frac{1}{\partial z} \left[\left(\frac{\partial \varphi}{\partial u}\right)^{2} + \left(\frac{\partial \varphi}{\partial v}\right)^{2} \right]$$

So we have

$$\left(\tau_{xy}\varphi\right)^2 = \frac{1}{\delta_{uu}} \left(\tau_{uv}\varphi\right)^2$$

under the conformal mapping.

The relation between the area element $dA_{\dot{X}\dot{Y}}$ in the z-plane and $dA_{\dot{U}\dot{V}}$ in the w-plane is found to be

$$dA_{xy} = dxdy$$

$$= \left(\partial_{uu}\partial_{uu}\right)^{1/2} dudv$$

$$= \partial_{uu}dudv$$

$$= \partial_{uu}dA_{uv}$$

and the power in each plane is

$$P_{xy} = S_{xy} dA_{xy} = \left[K \left(\nabla_{xy} \phi \right)^{2} \right] dA_{xy}$$

$$P_{uv} = S_{uv} dA_{uv} = \left[K \left(\nabla_{uv} \phi \right)^{2} \right] dA_{uv}$$

where P_{xy} , S_{xy} , and P_{uv} , S_{uv} are the power and the power density in the z-plane and the w-plane through the respective area elements.

Since

$$\begin{bmatrix} K \left(\nabla_{xy} \phi \right)^2 \end{bmatrix} dA_{xy} = \begin{bmatrix} K \frac{1}{\partial_{uu}} \left(\nabla_{uv} \phi \right)^2 \end{bmatrix} \partial_{uu} dA_{uv}$$
$$= \begin{bmatrix} K \left(\nabla_{uv} \phi \right)^2 \end{bmatrix} dA_{uv}$$

we conclude that

$$P_{xy} = P_{uv}$$

which says that under the conformal mapping the power in any area of the z-plane is the same as the power in the equivalent area of the w-plane.

Appendix C

DERIVATION OF EQUATION USED FOR COMPUTING PROPAGATION CONSTANT AND PHASE VELOCITY

Preceding page blank

Appendix C

DERIVATION OF EQUATION USED FOR COMPUTING PROPAGATION CONSTANT AND PHASE VELOCITY

In this appendix we derive an expression for the propagation constant of a T-M wave on a two-wire transmission line partly filled with dielectric (see Figure C-1).

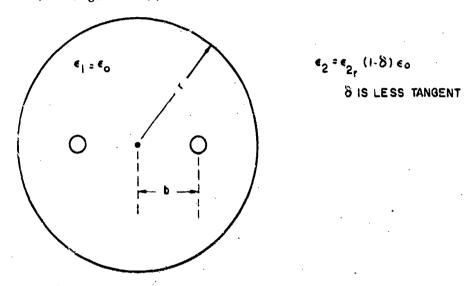


FIG. C-1 TRANSMISSION LINE GEOMETRY

We wish to find an approximation to the propagation constant for the quasi TEM wave on a two-wire transmission line that has, along its length, two dielectric materials (we are assuming one to be empty space, but this is not necessary). The boundary between the two dielectric materials is everywhere parallel to the conductor surfaces—i.e., parallel to the z-axis. In finding the propagation constant we will consider the case where the line is terminated in its characteristic impedance so that we have only a wave propagating in the positive z direction.

We will assume (or define) the power flow through any surface, closed or open, to be given by

Preceding page blank

$$P = \operatorname{Re} \int \hat{\mathbf{n}} \cdot \overline{\mathbf{S}} d\sigma ,$$

where n is the unit normal to the surface and

$$\overline{S} = \frac{1}{2} \stackrel{\sim}{E} \stackrel{\ast}{\vee} \stackrel{\ast}{H} \qquad .$$

In particular, the power flow do an open wire line is

$$P_{o} = \Re \int_{0}^{2\pi} \int_{0}^{\infty} \hat{z} \cdot \overline{S} r dr dC$$

Now consider, briefly, the TEM wave on the air-filled line with the same conductor configuration. For the lossless case, \overline{E} and \overline{H} are in phase and \overline{S} is real.

$$\hat{\mathbf{z}} \cdot \overline{\mathbf{S}} = \frac{\left|\overline{\mathbf{E}}\right|^2}{2\zeta_0} = \frac{\zeta_0 \left|\overline{\mathbf{H}}\right|^2}{2} \quad .$$

Hence

$$P_{o} = \frac{\zeta_{o}}{2} \int_{0}^{2\pi} \int_{0}^{\infty} |\bar{H}|^{2} r dr d\theta$$

Note also that

$$\widetilde{H} + \widetilde{H} = \widetilde{H} + \widetilde{H} + e$$

where the reference phase is taken at the point z = 0.

If we partly fill the line with a dielectric whose dielectric constant is of the order of magnitude of unity the H field will not change very much. We will, therefore, compute the propagation constant for the partly filled line from the TEM H field in the air filled line.

In either region of the partly filled line the transverse component of E is perpendicular to H, and H is related to E by

where

$$v = \alpha + i\theta$$

is the propagation constant we wish to find.

Thus

$$\hat{z} \cdot \bar{E} \times \bar{H} = \frac{\gamma}{j\omega\varepsilon} \bar{H} \cdot \bar{H} = \frac{\gamma}{j\omega\varepsilon} |\bar{H}|^2 e^{-2j\beta z}$$

Now let

$$v = \int_{\Omega}^{2\Pi} \int_{\Omega}^{\infty} \hat{z} \cdot \vec{E} \times \vec{H} r dr d\theta$$

which, upon substitution of the foregoing result, becomes

$$v = \frac{\gamma e^{-2j\theta z}}{jw} \int_{0}^{2\pi} \int_{0}^{\infty} \frac{1}{\epsilon} |\mu|^{2} r dr d\theta .$$

Note also that $v = P_t e^{-2j\beta z}$, where P_t is the power flowing on the partly filled line. Since both \tilde{E} and \tilde{H} vary as $e^{-\gamma z}$

and

Inerafore,

$$\gamma = -\frac{1}{2} \frac{\frac{dv}{dz}}{v}$$

To find dv/dz start with the identity

$$\int_{V} \nabla \cdot \bar{E} \times \bar{H} dv = \int_{\Sigma} \hat{n} \cdot \bar{E} \times \bar{H} d\sigma$$

where v is the volume outside of the conductors in a section of transmission line of length, h, and may extend radially to infinity. The integral over the cylindrical surface bounding the transmission line approaches zero as $r \to \infty$, hence

$$\begin{bmatrix} \int_{0}^{2\pi} \int_{0}^{\infty} \hat{z} \cdot \bar{E} \times \bar{H}rdrd\theta \end{bmatrix}_{z+h} - \begin{bmatrix} \int_{0}^{2\pi} \int_{0}^{\infty} \hat{z} \cdot \bar{E} \times \bar{H}rdrd\theta \end{bmatrix}_{z}$$

$$= \int_{V} \nabla \cdot \bar{E} \times \bar{H}_{dV} - \int_{0}^{\hat{n}} \cdot \bar{E} \times \bar{H}l\sigma \qquad .$$
conductor surface

When we divide by h and take the limit as h → o we obtain

$$\frac{dv}{dz} = \int_{0}^{2\pi} \int_{0}^{\infty} \nabla \cdot \tilde{E} \times \tilde{H}rdrd\theta - \int_{C} \hat{n} \cdot \tilde{E} \times \tilde{H}dS$$

The integral on the contour around the surface of the conductors

$$\int_{\mathbf{c}}^{\hat{\mathbf{n}}} \cdot \tilde{\mathbf{E}} \times \tilde{\mathbf{H}} d\mathbf{s} = \int_{\mathbf{c}} \tilde{\mathbf{E}} \cdot \tilde{\mathbf{H}} \times \hat{\mathbf{n}} d\mathbf{s} ,$$

and on the conductor surface

$$\vec{l} \times \hat{n} = \vec{J}_s = \hat{z}J_s$$

where \bar{J}_s is the surface current density. Now

$$\mathbf{E}_{\mathbf{z}} = \mathbf{Z}_{\mathbf{S}} \mathbf{S} \qquad ,$$

where

$$Z_s = R_s + jX_s = (1 + j) \sqrt{\frac{\omega \mu}{2\sigma}}$$

is the surface impedance and $\boldsymbol{\sigma}$ is the conductivity.

Hence

$$\int_{c} \hat{n} \cdot \tilde{E} \times \tilde{H} ds = (1 + j) R_{s} e^{-2j\beta z} \int_{c} |J_{s}|^{2} ds$$

and

$$\frac{dv}{dz} = \int_{0}^{2\pi} \int_{0}^{\infty} \nabla \cdot \vec{E} \times \vec{H}r dr d\theta - (1 + j)e^{-2j\hat{p}z} R_{s} \int_{c} |J_{s}|^{2} ds$$

If we use the vector identity

$$\nabla \cdot \vec{E} \times \vec{h} = \vec{H} \cdot \nabla \times \vec{E} - \vec{E} \cdot \nabla \times \vec{H}$$

and substitute from Maxwell's equations

$$\nabla \times \mathbf{H} = \mathbf{j}_{\mathbf{W}} \mathbf{E}$$

$$\nabla \times \mathbf{E} = \mathbf{j}_{\mathbf{W}} \mathbf{H}$$

we obtain

$$\Delta \cdot \mathbf{E} \times \mathbf{H} = -\mathbf{J} \mathbf{m} \{ \mathbf{n} \mathbf{H} \cdot \mathbf{H} + \mathbf{E} \mathbf{E} \cdot \mathbf{E} \}$$

When we assume

$$|\vec{E}_z| \ll |\vec{E}|$$

and use the relationship

$$\frac{1}{H} = \frac{j\omega \epsilon}{V} \nabla \times \bar{E}$$

we obtain

$$\nabla \cdot \vec{E} \times \vec{H} = -j\omega e^{-2j\beta z} \left\{ u - \frac{v^2}{\omega^2 \varepsilon} \right\} |H|^2$$

If we now let Σ_1 be the cross section surface over the air-filled region, and Σ_2 be that over the dielectric-filled region, we find

$$\frac{d\mathbf{v}}{d\mathbf{z}} = -j\omega \left[\left(\mu - \frac{\gamma}{\omega \varepsilon_0} \right) \int_{\Sigma_1} |\mathbf{H}|^2 d\sigma + \left(\mu - \frac{\gamma}{\omega^2 \varepsilon_2} \right) \int_{\Sigma_2} |\mathbf{H}|^2 d\sigma \right] e^{-2j\beta \mathbf{z}}$$

$$- (1 + j) R_s \int_{\mathbf{c}} |J_s|^2 ds e^{-2j\beta z}$$

and

$$Y = \frac{1}{2} \frac{\int_{\mathbb{R}^{2}} \left[H \right]^{2} d\sigma - \frac{Y}{\omega^{2}} \int_{\Sigma_{1}} \left[H \right]^{2} d\sigma - \frac{Y}{\omega^{2} \varepsilon_{2}} \int_{\Sigma_{2}} \left[H \right]^{2} d\sigma}{\frac{Y}{\int_{\mathbb{R}^{2}} \varepsilon_{0}} \int_{\Sigma_{1}} \left[H \right]^{2} d\sigma + \frac{Y}{\int_{\mathbb{R}^{2}} \varepsilon_{2}} \int_{\Sigma_{2}} \left[H \right]^{2} d\sigma}{\left[H \right]^{2} d\sigma}$$

$$+ (1 + j) \frac{\frac{Rs}{2} \int_{C} |J_{s}|^{2} ds}{\frac{P_{t}}{}}$$

If we define the attenuation constant due to the power dissipated in the conductors in the usual way, then the last term on the right is $(1+j)\alpha_{c}$, i.e.,

$$\alpha_{\rm e} = \frac{\frac{\rm Rs}{2} \int_{\rm e} \left| J_{\rm s} \right|^2 {\rm ds}}{P_{\rm s}}$$

where $\mathbf{P}_{\mathbf{t}}$ is the power carried in the wave traveling in the positive \mathbf{z} direction on the partly filled line.

Since we are assuming the H field on the partly dielectric filled line to be the same as that on a line with air as a dielectric, we can think of the integrals in the expression as the fractions of the power flowing in the corresponding regions of the air-filled line; thus,

$$P_{1} = \frac{\delta}{2} \int_{\Sigma_{1}} |H|^{2} d\sigma$$

$$P_2 = \frac{\delta}{2} \int_{\Sigma_2} |H|^2 d\sigma$$

and

$$P_0 = P_1 + P_2$$

If we now divide both the numerator and the denominator of the first term on the right by $\mathbf{P}_{\mathbf{Q}}$ and write

$$\frac{P}{P} = P$$

and

$$\frac{P_2}{P} = 1 - P$$

we obtain

$$\gamma^2 - 2(1 + j)\alpha_c \gamma = \frac{-A_c^2}{P + \frac{1}{\epsilon_{2r}}(1 - P)}$$

In this expression ϵ_{2r} may be complex:

$$\epsilon_{2r} = \epsilon_{2r}'(1 - j\delta)$$
,

where δ is the loss tangent of the dielectric material in region 2.

If the power loss due to the conductors is negligibly small, so that

$$\alpha_{c} \doteq 0$$
 ,

then the above equation reduces to

$$\gamma^2 = \frac{-\hbar^2}{p + \frac{1}{\epsilon_{2r}}(1 - P)}$$

We can solve this equation for ϵ_{2r} to yield

$$c_{2r} = \frac{-\gamma^2(1-p)}{\hbar^2 + \gamma^2 p}$$

As a check on the validity of the above expression for γ we can compare the result obtained from it with the propagation constant for the transverse magnetic mode in a special case that is relatively easy to solve. The coaxial transmission line with a coaxial dielectric sheath around the center conductor and an air space between that and the outer conductor is such a case. When we make the small argument approximations in the Bessel functions obtained in this solution, the two results are identical. We note also that this simple case can be approximated by assuming that the capacitance per unit length is equivalent to that

obtained by connecting those of the two regions in series and that the conductance per unit length is that for the air-filled line. This approximation also yields the identical result for γ .

Appendix D

DERIVATION OF RELATIVE POWER DENSITY IN BOTH x AND y POLARIZATIONS

DERIVATION OF RELATIVE POWER DENSITY IN BOTH x AND y POLARIZATIONS

For a TEM wave the electric field intensity \vec{E} is given by

$$\vec{E} = - \varphi_z \nabla_{uv} F$$

where ϕ_z is a function only of z, and F is a function of u, v satisfying

$$\nabla_{\mathbf{u}\mathbf{v}}^{\mathbf{2}}\mathbf{F} = \mathbf{0}$$

and

$$\frac{\partial F}{\partial S} = 0$$

on the surface S of the conductors.

Let u, v be the bipolar coordinates. 14 Then we find

$$F = Au$$

$$\vec{E} = A\phi_z \left(\frac{\cosh u - \cos v}{c} \right) \hat{u}$$

$$\hat{\mathbf{u}} = \frac{1 - \cosh \mathbf{u} \cos \mathbf{v}}{\cosh \mathbf{u} - \cos \mathbf{v}} \hat{\mathbf{x}} - \frac{\sinh \mathbf{u} \sin \mathbf{v}}{\cosh \mathbf{u} - \cos \mathbf{v}} \hat{\mathbf{y}}$$

SO.

$$\vec{E} = \frac{A\phi_z}{C} (1 - \cosh u \cos v) \hat{x} - \frac{A\phi_z}{C} (\sinh u \sin v) \hat{y}$$

The ratio of the y component of \vec{E} to the x component, $|E_y|/|E_x|$, is

$$\frac{|E_{y}|}{|E_{x}|} = \frac{\sinh u \sin v}{\cosh u \cos v - 1}.$$

Preceding page blank

Now,

$$x = \frac{c \sinh u}{\cosh u - \cos v}$$

$$y = \frac{c \sin v}{\cosh u - \cos v}$$

Using the additional identities

$$\sin^2 v + \cos^2 v = 1$$

$$\cosh^2 u - \sinh^2 u = 1$$

we can solve for $\sin v$, $\cos v$, $\sinh u$, and $\cosh u$ in terms of x, y. This results in,

$$\sin v = \frac{2cy}{\sqrt{(x^2 + y^2 - c^2)^2 + (2cy)^2}}$$

$$\cos v = \frac{(x^2 + x^2 - c^2)}{\sqrt{(x^2 + y^2 + 1)^2 + (2cy)^2}}$$

$$\sinh u = \frac{2cx}{\sqrt{(x^2 + y^2 - c^2)^2 + (2cy)^2}}$$

$$\cosh u = \frac{(x^2 + y^2 + c^2)}{\sqrt{(x^2 + y^2 - c^2)^2 + (2cy)^2}}$$

Substituting the above expressions in the expression for $|E_y|/|E_\chi|$, we find

$$\frac{\left|E_{y}\right|}{\left|E_{x}\right|} \approx \left|\frac{2xy}{x^{2}-y^{2}-c^{2}}\right|$$

Normalizing the coordinates with c, we have

$$\frac{|E_y|}{|E_x|} = \left| \frac{2xy}{x^2 - y^2 - 1} \right|$$

$$\frac{|E_y|^2}{|E_x|^2} = \frac{4x^2y^2}{(x^2 - y^2 - 1)^2} .$$

Since the power density P_{x} and V_{y} in x- and y-polarization, respectively, are given by

$$P_{x} = \frac{\left|E_{x}\right|^{2}}{2\zeta}$$

$$P_y = \frac{|E_y|^2}{26}$$

we have,

$$\frac{P_y}{P_k} = \frac{|E_y|^2}{|E_k|^2} = \frac{4x^2y^2}{\left(x^2 + y^2 - 1\right)^2} , \qquad (0-1)$$

The relation between the total power density P and P, P, for the TEM wave is found to be

it i beene thei

$$P = \frac{4\pi}{\left(x^2 + y^2 - 1\right)^2 + 4x^2y^2}$$

Normalizing the coordinates with c, we have

$$\frac{\left|E_{y}\right|}{\left|E_{x}\right|} = \left|\frac{2xy}{x^{2} - y^{2} - 1}\right|$$

$$\frac{|E_y|^2}{|E_x|^2} = \frac{4x^2y^2}{(x^2 - y^2 - 1)^2}$$

Since the power density $\mathbf{P}_{\mathbf{x}}$ and $\mathbf{P}_{\mathbf{y}}$ in x- and y-polarization, respectively, are given by

$$P_{x} = \frac{\left|E_{x}\right|^{2}}{2\zeta}$$

$$P_{y} = \frac{\left|E_{y}\right|^{2}}{2\zeta}$$

we have,

$$\frac{P_{x}}{P_{x}} = \frac{|E_{y}|^{2}}{|E_{x}|^{2}} = \frac{4x^{2}y^{2}}{(x^{2} + y^{2} - 1)^{2}} \qquad (D-1)$$

The relation between the total power density P and P , P for the TEM wave is found to be

$$P = P_{x} + P_{y} .$$

It is known that

$$P = \frac{4B}{\left(x^2 + y^2 - 1\right)^2 + 4x^2y^2}$$

whore

50,

$$P_{x} + P_{y} = \frac{4B}{\left(x^{2} + y^{2} - 1\right)^{2} + 4x^{2}y^{2}} . \tag{D-2}$$

Solving (D-1) and (D-2) simultaneously, we get

$$P_{y} = \frac{16Bx^{2}y^{2}}{\left[\left(x^{2} + y^{2} - 1\right)^{2} + y^{2}\right]^{2}}$$

$$P_{x} = \frac{4B(x^{2} + y^{2} - 1)^{2}}{\left[\left(x^{2} + y^{2} - 1\right)^{2} + 4x^{2}y^{2}\right]^{2}}$$

1. The Plot of P_X

For a contour of constant P_{χ} , let

$$P_{x} = P_{xk} = constant$$

and

$$D_{x}^{2} = \frac{4B}{P_{xk}}$$

thon

$$\frac{\left[\left(x^2 + y^2 - 1\right)^2 + 4x^2y^2\right]^2}{\left(x^2 + y^2 - 1\right)^2} = D_x^2.$$

The power in dB is given by

2. The Plot of Py

For a contour of constant Py, let

$$P_y = P_{yk} = constant$$

and

$$D_y^2 = \frac{4B}{P_{yk}}$$

then

$$\frac{\left[\left(x^2 + y^2 - 1\right)^2 + 4x^2y^2\right]^2}{4x^2y^2} = D_y^2.$$

The power in dB is given by

$$P_y = 10 \ lo_{x_{10}} \frac{1}{D_y}$$

Appendix E

ANALYSIS OF ADDED CAPACITANCE ON A TRANSMISSION LINE TO APPROACH A GIVEN EFFECTIVE DIELECTRIC CONSTANT

Preceding page blank

Appendix E

ANALYSIS OF ADDED CAPACITANCE ON A TRANSMISSION LINE TO APPROACH A GIVEN EFFECTIVE DIELECTRIC CONSTANT

The following computations were made as a check on the validity of representing a transmission line with discrete capacitive scatterers (shunt capacitors) as a line with a higher dielectric constant and no shunt capacitors.

For the TEM wave on a two-conductor transmission line:

the voltage,
$$V = \int_{\frac{1}{2}}^{\frac{1}{2}} \frac{conductor}{dr} \frac{2}{conductor}$$

the total current,
$$I = \int_{0}^{\infty} \frac{1}{H^2 ds}$$
 conductor 1 or 2

and the charge per unit length

$$q = \int \hat{n} \cdot \overline{D} ds$$
conductor 1 or 2

Since

$$\hat{n} \times \bar{E} = 0$$

and
$$\hat{n} \cdot \hat{H} = 0$$

at the conductor surface, and since

$$|E| = G|H|$$

whore

\$\zerta \text{ the modulys of the impedance of the modium}

und

$$\tilde{D} = \epsilon \tilde{E}$$

Preceding page blank

$$q = \varepsilon \int |E| ds$$
 conductor 1

Therefore, the characteristic impedance

$$R_{c} = \frac{V}{I} = \sqrt{\frac{\mu_{r}}{\epsilon_{r}}} \zeta \frac{V}{\int \frac{|E| ds}{conductor 1}}$$

and the capacitance per unit length is

$$C = \frac{q}{v} = \frac{e \cdot e}{r \cdot o} \int |E| ds$$
 conductor 1

The added capacitance per unit length due to increasing the dielectric constant from 1 to ϵ_{r} is

$$C' = \frac{(\varepsilon_r - 1)\varepsilon}{V} |E| ds$$
conductor 1

Now suppose we place n capacitors per wavelength (λ) on an air dielectric line, each capacitor having a capacitance

$$C_s = \frac{\lambda c}{n}$$
.

Then, as a increases, the equivalent dielectric constant should approach ϵ_{r} and the relative permeability should approach unity.

On the air line, each shunt capacitor has a normalized admittance.

whoro

f = frequency, in Hz

$$Y_{s} = j \frac{2\pi f \lambda}{h} C' R_{c(air)}$$

$$Y_{s} = j \frac{2\pi v_{o}}{n} (\epsilon_{r} - 1) \epsilon_{o} \zeta_{o}$$

where

V = phase velocity in air

$$Y_s = j\frac{2\pi}{n} (\varepsilon_r - 1)$$

In our computation we let $\boldsymbol{C}_{\mathbf{S}}$ have a small loss factor, $\delta,$ such that

$$\epsilon_{\mathbf{r}} = \epsilon_{\mathbf{r}} (1 - j\delta)$$
.

For computations with equally spaced uniform-size capacitors two circuits were used (see Figure E-1).

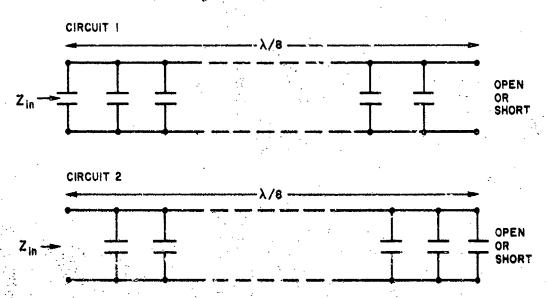


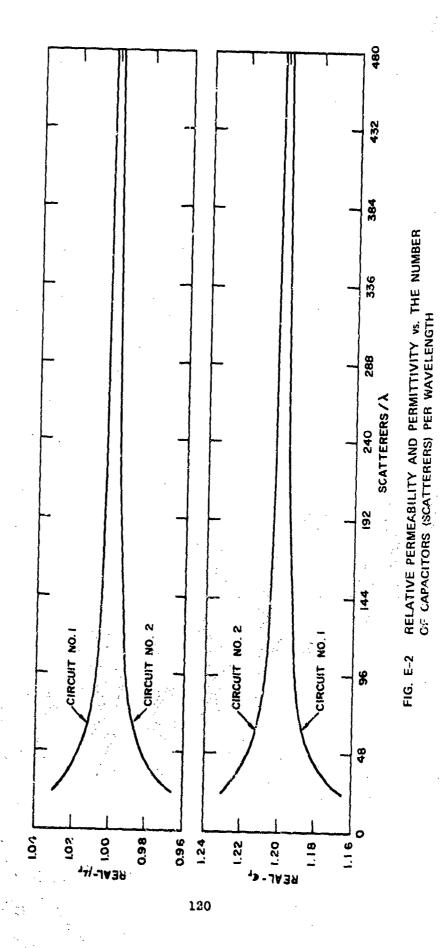
FIG. E-1 EQUIVALENT CIRCUITS FOR CAPACITIVELY LOADED TRANSMISSION LINE

Example computations of $\epsilon_{\bf r}'$ and $\mu_{\bf r}'$ were made using equally spaced uniform-size capacitors in Circuits 1 and 2 for the case:

n = a'24

$$\epsilon_{r} = 1.2(1 - j0.05)$$
 $a = 1 \text{ to } 20$

The results are plotted in Figure E-2. Notice that when the number of capacitors (scatterers) per wavelength is large that both circuits yield



the same (and correct) answer. On the other hand, when the number of scatterers is small, both circuits exhibit a bias. Circuit 2, more nearly the case in actual field measurements described in Ref. 13, where the vegetation was cleared from around the bridge input to the line, yields results slightly high for $e_{\mathbf{r}}'$ and slightly low for $p_{\mathbf{r}}'$. Notice that, for a given number of scatterers, the value of either ϵ_n' or μ_n' obtained by averaging the results from Circuits 1 and 2 is the correct value to use in the slab model. This implies that, because of incomplete spatial sampling (i.e., never having a tree trunk right at the bridge input), the average of the observed values of μ_n' given in Ref. 13 should be somewhat less than unity -- and indeed such was the case. Nevertheless, contrary to the discussion in Ref. 13, the true value of $\mu_{\mathbf{r}}^{\prime}$ in the forest being measured probably was unity, and the assumption $\mu_{\mathbf{r}1}'$ = 1 should be used in forest-slab-model computations. In addition, the true value of en probably always was greater than (or equal to) unity. Finally, future measurements should include complete spatial sampling relative to the geometry of the scatterers.

Computations also were made for the case of random scatterer size and location. For the random-size scatterers, the average value of Y was set equal to Y above. Except for increased spread of the computed data points, essentially the same conclusion was reached: Namely, that a transmission line with discrete scatterers placed along it can be represented as a line immersed in a scatterer-free region of higher dielectric constant--provided there is a sufficient number of scatterers present (per wavelength) down the line.

Private communication, H. W. Parker.

REFERENCES

- 1. D. J. Pounds and A. H. LaGrone, "Considering Forest Vegetation as an Imperfect Dielectric Slab," Report 6-53, Contract AF 19(604)-8038, Project 4603, The Electrical Engineering Research Laboratory, University of Texas, Austin, Texas (1963), UNCLASSIFIED, AD-410 836.
- 2. John Taylor, "A Note on the Computed Radiation Patterns of Dipole Antennas in Dense Vegetation," Special Technical Report 16, Contract DA 36-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menlo Park, California (February 1966), UNCLASSIFIED, AD-487 495.
- 3. D. L. Sachs and P. J. Wyatt, "A Conducting-Slab Model for Electromagnetic Propagation within a Jungle Medium," Technical Memorandum 376 and Internal Memorandum IMR-471, Defense Research Corporation, Santa Barbara, California (1966). [Also appears in Radio Science, Vol. 3 (New Series), No. 2, pp. 125-134 (February 1968).]
- 4. D. L. Sachs, "A Conducting Slab Model for Electromagnetic Propagation within a Jungle Medium II," Internal Memorandum IMR-471, Defense Research Corporation, Santa Barbara, California (30 September 1966).
- 5. Theodor Tamir, "On Radio-Wave Propagation in Forest Environments,"

 IEEE Trans. on Antennas and Propagation, Vol. AP-15, No. 6, pp.

 806-817 (November 1967).
- 6. James R. Wait, "Radiation from Dipoles in an Idealized Jungle Environment," Radio Science, Vol. 2 (New Series), No. 7, pp. 747-750 (July 1967).
- 7. Ching-Chun Han, "The Measurement of Electrical Properties of a Forest," Master Thesis, Department of Electrical Engineering, University of South Carolina, Columbia, South Carolina (1967).
- 8. H. W. Parker and G. H. Hagn, "Feasibility Study of the Use of Open-Wire Transmission Lines, Capacitors, and Cavities to Measure the Electrical Properties of Vegotation," Special Technical Report 13, Contract DA 36-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menlo Park, California (August 1966), UNCLASSIFIED, AD-489 294.
- 9. G. H. hagn, H. W. Parker, and E. L. Younker, "Research-Engineering and Support for Tropical Communications," Semiannual Report 5, covering the period 1 April through 30 September 1965, Contract DA 36-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menlo Park, California (May 1966), UNCLASSIFIED, AD-486

- 10. G. H. Hrgn, E. L. Younker, and H. W. Parker, "Research-Engineering and Support for Tropical Communications," Semiannual Report 6, covering the period 1 October 1965 through 31 March 1966, Contract DA 38-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menlo Park, California (June 1966), UNCLASCIFIED, AD-653 608.
- 11. E. L. Younker, G. H. Hagn, and H. W. Parker, "Research-Engineering and Support for Tropical Communications," Semiannual Report 7, covering the period 1 April through 30 September 1966, Contract DA 36-039 AMC-00040(F), SRI Project 4240, Stanford Research Institute, Menlo Park, California (September 1966), UNCLASSIFIED, AD-653 615.
- 12. E. L. Younker, G. H. Hagn, and H. W. Parker, "Research-Engineering and Support for Tropical Communications," Semiannual Report 8, covering the period 1 October 1966 through 31 March 1967, Contract DA 36-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menlo Park, California (May 1967), UNCLASSIFIED, AD-675-459.
- 13. H. W. Parker and Withan Makarabhiromya, "Electric Constants Measured in Vegetation and in Earth at Five Sites in Thailand," Special Technical Report 43, Contract DA 36-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menlo Park, California (December 1967), UNCLASSIFIED, AD-674-740.
- 14. Hugh H. Skilling, Electric Transmission Lines (McGraw-Hill Book Co., Inc., New York, New York, 1951).
- 15. G. H. Hagn, G. E. Barker, H. W. Parker, J. D. Hice, and W. A. Ray, "Preliminary Results of Full-Scale Pattern Measurements of Simple VHF Antennas in a Eucalyptus Grove," Special Technical Report 19, Contract DA 36-039 AMC-00040(E), SRI Project 4240, Stanford Research Institute, Menio Park, California (January 1966), UNCLASSIFIED, AD-484 239.
- 16. D. G. Neal, "Statistical Description of the Forests of Thailand," MRPC Report 67-019, Miliary Research and Development Center, Bangkok, Thailand (May 1967).